Non-Parametric Morphology Statistics as Galaxy Classifiers

The Evolution of Galaxy Structure Over Cosmic Time, Conselice 2014 Presented by Scott Wilkinson

Morphology Classes





CAS - Concentration

$$C = 5\log_{10}\left(\frac{r_{80}}{r_{20}}\right)$$

Kent 1985; Conselice 2003

Sometimes calculated as:

- C = r(75) / r(25) (de Vaucouleurs 1977)
- C = r(90) / r(50) (Strateva et al. 2001)
- $C = 5 \log (r(70) / r(30))$

"Total flux" can either be flux within,

- 1.5 Rpetro (Conselice 2003)
- 2 Rpetro (Bershady 2000)



CAS - Concentration

Concentration can be used as a simple single-metric classifier of galaxy morphology.



Strateva et al. 2001

CAS - Asymmetry



CAS - Smoothness (Clumpiness)

$$S = 10 \times \left[\left(\frac{\Sigma(I_{x,y} - I_{x,y}^{\sigma})}{\Sigma I_{x,y}} \right) - \left(\frac{\Sigma(B_{x,y} - B_{x,y}^{\sigma})}{\Sigma I_{x,y}} \right) \right]$$

Warning: sometimes no x10 (Lotz et al. 2004, 2008)



$$\sigma = 0.3 \cdot 1.5 \times r(\eta = 0.2)$$

I-B

В

Sometimes 0.2 (Conselice 2009) or 0.25 (Lotz et al. 2004)

$$\eta(R) = \frac{I(R)}{\langle I(\langle R) \rangle}$$

"[T]he clumpiness parameter (S) is incalculable due to limitations in the resolution of our images (PSF ~ 0. 3")"(Bluck et al. 2012).

CAS - Summary

Galaxy type	Concentration (R)	Asymmetry (R)	Clumpiness (R)	
Ellipticals	4.4 ± 0.3	$0.02~\pm~0.02$	0.00 ± 0.04	
Early-type disks (Sa-Sb)	3.9 ± 0.5	$0.07~\pm~0.04$	0.08 ± 0.08	
Late-type disks (Sc-Sd)	3.1 ± 0.4	0.15 ± 0.06	0.29 ± 0.13	
Irregulars	2.9 ± 0.3	0.17 ± 0.10	0.40 ± 0.20	
Edge-on disks	3.7 ± 0.6	0.17 ± 0.11	0.45 ± 0.20	-
ULIRGs	3.5 ± 0.7	0.32 ± 0.19	0.50 ± 0.40	A(R
Starbursts	2.7 ± 0.2	0.53 ± 0.22	0.74 ± 0.25	
Dwarf ellipticals	2.5 ± 0.3	0.02 ± 0.03	0.00 ± 0.06	





Conselice CJ. 2014. Annu. Rev. Astron. Astrophys. 52:291–337



R Conselice CJ. 2014. Annu. Rev. Astron. Astrophys. 52:291–337 0.6 0.8

"When using these three morphological parameters, all known nearby galaxy types can be distinctly separated and distinguished in structural space" (Conselice 2003, 2014).

G-M20: Gini



Gini Coefficient By Country 2021

$$G = \frac{1}{\bar{X}n(n-1)} \sum_{i=1}^{n} (2i - n - 1)X_i$$

G=1, if all the light is concentrated in a single pixel G=0, if all the light is equally distributed across the galaxy

All three images have the same value of G...









Abraham et al. 2002

Gini-M20: M20

$$M_{\text{tot}} = \sum_{i}^{n} M_{i} = \sum_{i}^{n} f_{i} \left[(x_{i} - x_{c})^{2} + (y_{i} - y_{c})^{2} \right]$$
$$M_{20} \equiv \log 10 \left(\frac{\sum_{i} M_{i}}{M_{\text{tot}}} \right), \text{ while } \sum_{i} f_{i} < 0.2 f_{\text{tot}}$$

M20 measures the spatial variance of the brightest 20% of pixels (relative to the whole galaxy)



Gini-M20

In tandem, Gini and M20 can be used to classify galaxies, too.

Pan-STARRS 0.8 5.0 0.7 4.5 0.7 Gini Coefficient, G × Concentration, - 3.5 Δ 0.6 0.6 -G (R) 0.5 E/S0/Sa 0.5 0.4 - 2.5 Sb/Sc/Sd/Irr X X 0.4 Lotz et al. 2004 L 2.0 Rodriguez-Gomez et al. (2019) 0.3 --2 -3-1 -0.5 -3.0 -2.5-2.0-1.5-1.0 M_{20} (R) M_{20}

Non-parametric Morphology of Mergers



Visual Assessment



11/16

Lotz et al. 2004

Merger Fraction through Cosmic Time



Since Conselice 2014...

Some new non-parametric morphology statistics:

- MID statistics (Freeman et al. 2013)
- Shape Asymmetry (Pawlik et al. 2016)
- Outer Asymmetry (Pawlik et al. 2016)

Relative Statistic Importance: J Band





An attempt to combine the metrics...

Trained on a suite of hydrodynamical simulations with SDSS imaging realism applied, Nevin et al. (2019) uses Linear Discriminant Analysis to combine metrics and identify mergers...

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 LD1_{major} = 0.69 \text{ Gini} + 3.84 C + 5.78 A + 13.14 A_S \\ - 3.68 \text{ Gini} * A_S - 6.5 C * A_S - 6.12 A * A_S \\ - 0.81,
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The LDA can't be applied to other surveys without retraining...

Problems not Addressed

Foreground star contamination can increase G, M20, A, and S and decrease C.

Effects of PSF FWHM, pixel scale, depth, wavelength

Observability timescale

Can you reliably compare these statistics over cosmic time and in different imaging?



C = 1.68 A = 0.88 S = 0.18 G = 0.64 M20 = -0.944





Machine Learning



Galaxy morphology is as nuanced as the physics that drives it

Spirals

The field is moving away from non-parametric morphology statistics and towards machine learning algorithms.

superior confidence ($16 \le i < 18$ and z < 0.25)

Questions?

Additional Figures

