

THE DISTRIBUTION OF EXTRAGALACTIC NEBULAE *

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Abstract. Counts of extragalactic nebulae have been made on plates taken with the 20-inch Carnegie astrograph of the Lick Observatory. The area of the sky for which the results are published in the present paper extends in right ascension from 12^{h} to 18^{h} and in declination from -20° to $+20^{\circ}$. The limiting magnitude of about 18.4 has been made as nearly as possible constant over this entire region through the use of uniform procedures and the application of corrections for systematic errors. The principal data are given in a table containing the counted numbers of nebulae in each square degree together with corrections to reduce these numbers to a uniform basis, and the results are portrayed by means of a chart giving contours of equal numbers of nebulae per square degree.

In addition to a very irregular boundary of the zone of avoidance, several more or less detached areas of galactic obscuration are apparent on the chart. In higher latitudes, where the effect of galactic obscuration should be small, the distribution of nebulae is still so far from random as to suggest strongly that clustering is a very general feature of the distribution.

The distribution of surface density of nebulae in Coma-type clusters has been studied in a very preliminary way and is found to be well represented by de Vaucouleurs' empirical formula for the distribution of light in elliptical nebulae. The association of clusters to form larger aggregations or clouds of nebulae seems to be a rather general feature of the distribution.

I. INTRODUCTION

The problem of nebular distribution may be considered from two aspects. One is concerned with the way in which the nebulae are distributed over the surface of the sky, and the other with their distribution in depth. Extensive nebular counts, or surveys, provide the observational material for both investigations but the approach is very different.

A survey in depth requires that nebulae be counted in properly selected sample areas to specific limiting magnitudes that cover as wide a range as possible. Nearly twenty years ago Hubble carried out the principal survey in depth that has been made to date.¹ More recently he has outlined the direction that should be taken in an improved and definitive survey.² The requirements are very severe, for the limiting magnitudes must be determined on a highly accurate scale. In order to correct for the larger red shifts, the intensity distribution in the spectra of the nebulae must be known to much shorter wave lengths than those covered by the adopted magnitude system. Since it is not possible to determine the intensity distribution in the far ultraviolet, it is desirable to make the survey in the region of longer wave lengths. Even if proper allowance can be made for the spectral energy distribution, the corrections for the red shift depend on whether or not the shift is due to recessional velocity. It is not at present clear what allowance should be made for the excess reddening of very distant nebulae as observed by Stebbins and Whitford.³ Observers at the Mount Wilson Palomar Observatories are laying the foundation for what it is hoped will be a definitive survey in depth.⁴ When this survey is complete, it will provide essential information not only on a pos-

sible large-scale radial density gradient of the universe, but also on the nature of the red shift and on the curvature of space.

A study of the surface distribution of the extragalactic nebulae requires quite a different observational approach. For this purpose the plates should cover a very substantial connected area of the sky, but the counts may be restricted to a single limiting magnitude. This limiting magnitude need not be determined with high precision but it should be constant over the region surveyed. Smaller-scale inhomogeneities can be observed than those revealed by a survey in depth.

Suitable material for a nebular survey over the surface of the sky is provided by a series of 1246 plates taken with the 20-inch Carnegie Astrograph at the Lick Observatory. These plates are the first of two series in a proper motion program originally planned by Wright.⁵ It is intended that the second series shall be taken after an interval of some decades. The plates cover the entire sky north of declination -23° , with uniform exposures of two hours centered on the meridian. Perhaps their greatest advantage lies in the fact that each plate covers an area 6° square with the plate centers not more than 5° apart in each coordinate. Thus each plate has a generous overlap with at least three and usually with four of its neighbors. Nebulae in the overlaps are most useful in reducing the counts to a common standard.

The number of nebulae photographed to a limiting magnitude of 18.3 or 18.4 is of the order of a million. Nebular counts were started by the authors late in 1947, and in the interest of uni-

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formity, all the plates are now being counted by them. Five of the earlier plates were counted by Mayall. The counts are about 44 per cent complete and are being continued as rapidly as possible.

For purposes of discussion the sky has been divided into nine areas. Areas I to IV inclusive cover 6^h intervals starting at 0^h and lying between -23° and $+20^\circ$. Areas V to VIII cover the same intervals in right ascension from declination $+20^\circ$ to $+60^\circ$. Area IX comprises all of the polar region north of $+60^\circ$. Only the counts in Area III, $\alpha = 12^h$ to 18^h , $\delta = -23^\circ$ to $+20^\circ$, have been completely reduced to date. The results of this discussion form the subject of the present paper.

II. THE PHOTOGRAPHS

The photographic plates are seventeen inches square and cover a field of slightly more than 36 square degrees. They were coated by the Eastman Kodak Research Laboratory with emulsion of type 103a-O. The five emulsions used in Area III were uniform in average sensitivity to a very satisfactory degree, with an extreme range of less than 0.2 mag. in average limiting magnitude, as determined from the nebular counts. Care was taken to maintain uniformity in development and to guard against deterioration of the plates in storage.

The plate centers for the entire program are referred to the equator and equinox of 1950. From $\delta = -20^\circ$ to $\delta = +35^\circ$, the centers are spaced 20^m apart, starting at $\alpha = 0^h$. From $\delta = +40^\circ$ to $\delta = +50^\circ$, the increments are 24^m. North of $\delta = +50^\circ$ the increments are as follows: for $\delta = +55^\circ$, 32^m; $\delta = +60^\circ$, 36^m; $\delta = +65^\circ$, 40^m; $\delta = +70^\circ$, 48^m; $\delta = +75^\circ$, 60^m; $\delta = +80^\circ$, 90^m; $\delta = +85^\circ$, 144^m. All plates are centered accurately with the errors seldom exceeding 1' in either coordinate. While the usable field on each plate is 6° square, the plate centers are no more than 5° apart, so that except for the southern band of plates, one degree around the edge of each plate is duplicated on adjacent photographs.

Each exposure was started 1^h1^m before the center of the field crossed the meridian. At the end of an hour the exposure was interrupted for 2 minutes. During this interval a one-minute exposure centered on the meridian was taken with the telescope shifted approximately 1' in right ascension. The telescope was then returned to its original position for the second hour exposure.

A coarse wire grating of $\frac{1}{4}$ -inch spacing placed in front of the lens was used throughout. This grating gives first-order images 4 magnitudes fainter than the primary images and separated from them by 0'.24. It reduces the limiting magnitude by 0.3 mag. Both the grating images and the short exposures are a slight hindrance in the nebular work, but they are important in an astrometric study of the material when the positions of bright and faint stars are compared.

Occasionally exposures were interrupted by clouds. Some plates of deficient effective exposures were used in the survey if the deficiency did not exceed 20^m. In such cases suitable corrections were applied to the counts.

III. THE COUNTS

The uncorrected nebular counts per square degree for Area III are given in Table I. The numbers are arranged so that north is at the top, east to the left. Plates in each 5° zone of declination are tabulated as separate groups. Above each block of counts representing the 36 square degrees on a plate are certain designations pertaining to that plate. The plate number is given at the upper left. Below this is the initial of the observer who counted the plate, followed by a small letter indicating the emulsion. The right ascension of the plate is given at the upper right and below it is the complete plate factor, F, defined below. Several plate numbers are followed by asterisks, which refer to the notes following the table. The notes list the plates deficient in effective exposure time and those omitted from the solution for the various correction factors because of outstanding discrepancies with their overlapping neighbors.

Although the numbers of nebulae per square degree are tabulated, the original counts were actually recorded in 10' squares. The counting procedure is in general uniform throughout. The plate is mounted in a frame with a motion in the north-south or y direction. The observing microscope moves in the east-west or x coordinate. Scales reading to 1' permit the fairly accurate location of the area to be counted. In the focal plane of the microscope there is a square 10' on a side defined by cross hairs. This is first centered on the northwest 10' square of the plate, and the number of nebulae in that square is counted and recorded. Counts are made across the plate by 10' intervals from west to east. Then the plate is moved south by successive 10' intervals and the process is repeated in the same

TABLE I. AREA III, UNCORRECTED COUNTS OF NEBULAE PER SQUARE DEGREE

$\delta = -20^\circ$					788 $12^h 00^m$ S b 1.022	1512 $12^h 20^m$ S h 0.953	469 $12^h 40^m$ S a 0.822	476* $13^h 00^m$ S a 0.999
					35 36 38 27 22 36	56 73 61 41 30 33	56 49 50 51 32 50	50 53 62 70 146 40
					68 69 37 49 73 40	41 46 35 37 59 51	77 53 43 45 42 60	54 72 49 61 70 56
					51 44 34 49 51 36	31 77 36 24 33 49	61 61 54 57 48 68	57 63 84 44 40 51
					31 39 54 67 41 62	42 39 19 25 24 27	77 65 50 50 42 59	57 72 50 33 51 47
21 34 36 53 30 15	31 50 52 47 31 18	82 81 72 45 46 57	60 74 49 53 40 58					
29 13 23 28 14 10	39 31 32 29 29 14	59 69 54 45 49 51	37 57 47 46 60 54					
803 $13^h 20^m$ S b 0.892					1164 $13^h 40^m$ W e 0.834	1574** $14^h 00^m$ S h 1.780	789** $14^h 20^m$ W b 0.415	1590 $14^h 40^m$ S h 0.978
					50 54 35 74 50 38	34 27 33 30 30 59	30 31 48 32 35 33	10 24 21 35 12 5
					33 44 30 39 41 63	30 33 57 48 25 24	43 40 51 32 44 44	19 23 36 18 15 27
					48 26 58 20 48 60	63 49 69 67 52 38	52 59 50 62 39 46	21 32 21 15 16 21
					39 83 41 33 47 39	35 31 38 33 50 48	32 59 47 37 24 33	26 31 20 27 11 15
43 55 33 56 40 53	22 25 24 25 37 51	16 19 23 27 18 7	23 33 38 15 21 16					
45 29 49 45 49 37	35 42 40 31 41 44	16 20 23 28 19 11	17 17 19 20 13 7					
470 $15^h 00^m$ W a 0.825					852* $15^h 20^m$ W b 0.885	1254** $15^h 40^m$ W f 1.522	1604 $16^h 00^m$ S h 1.047	1208 $16^h 20^m$ S e 0.879
					25 15 5 12 16 21	34 23 24 28 20 25	8 5 17 7 11 13	2 1 2 0 2 2
					19 14 13 22 18 21	19 9 9 16 11 15	5 5 13 10 6 14	2 4 2 3 1 3
					35 26 16 33 24 29	22 12 10 15 16 8	10 3 9 12 6 10	0 1 0 1 1 3
					35 25 20 22 10 31	20 24 17 16 17 21	6 4 5 1 10 5	1 0 0 0 2 1
39 23 22 28 25 31	18 29 17 14 15 21	4 5 9 9 14 22	1 1 1 1 1 5					
23 20 19 20 32 40	35 31 30 16 27 27	19 12 13 15 32 37	0 0 0 2 10 0					
874 $16^h 40^m$ S b 1.000					888 $17^h 00^m$ S b 0.879	529 $17^h 20^m$ S a 0.914	526 $17^h 40^m$ S a 0.914	487 $18^h 00^m$ S a 0.914
					0 2 0 1 1 2	0 0 0 1 2 0	0 0 0 0 0 0	0 0 0 0 0 0
					0 0 1 1 2 0	1 1 3 6 3 1	1 0 0 1 2 1	0 0 0 1 0 0
					3 1 0 1 6 1	0 1 3 3 0 0	0 0 0 0 5 1	0 0 0 0 0 0
					5 3 5 2 1 1	1 1 5 2 3 7	0 0 0 0 1 0	0 0 0 0 2 0
0 1 0 0 1 2	0 0 0 2 2 0	0 0 0 0 0 0	0 0 0 0 0 0					
2 1 0 0 0 0	0 0 0 1 2 0	0 0 0 1 0 0	0 1 0 0 0 0					
$\delta = -15^\circ$					1532 $12^h 00^m$ S h 0.975	1568** $12^h 20^m$ S h 1.695	812 $12^h 40^m$ W b 1.155	774 $13^h 00^m$ S b 0.844
					45 39 49 42 54 52	21 24 29 57 27 19	72 44 35 37 15 22	68 34 51 78 119 76
					63 66 54 44 45 39	32 44 39 79 44 30	41 32 24 27 15 45	58 55 91 111 152 58
					49 45 41 37 77 57	35 26 40 35 27 28	139 80 34 27 54 34	56 82 66 92 111 169
					49 39 29 23 49 76	35 24 46 26 23 17	165 50 42 49 22 31	72 82 85 128 121 193
51 52 29 38 48 65	25 30 31 19 14 15	48 40 36 45 19 17	67 86 143 115 134 51					
47 36 50 39 28 32	24 37 30 16 15 6	47 34 51 46 27 43	63 54 64 102 154 33					
814 $13^h 20^m$ S b 0.977					482 $13^h 40^m$ S a 1.077	1223 $14^h 00^m$ W f 0.716	1587 $14^h 20^m$ S h 1.329	1601 $14^h 40^m$ S h 1.202
					73 66 82 68 56 68	56 37 46 59 52 50	28 9 13 13 12 18	14 16 21 23 12 18
					87 62 46 43 55 55	52 66 56 42 48 71	14 18 14 13 23 25	18 32 25 18 22 12
					90 40 41 59 54 45	63 49 41 47 36 59	17 21 36 20 14 19	31 17 19 17 13 16
					50 53 37 56 63 40	49 34 46 34 38 23	14 16 31 30 24 20	30 22 16 19 18 10
29 47 55 113 48 31	25 26 34 37 33 19	17 20 50 44 13 8	16 16 24 37 16 15					
26 29 32 57 55 28	27 27 34 23 22 24	6 13 27 13 12 9	13 21 21 18 4 2					
475 $15^h 00^m$ S a 0.788					841 $15^h 20^m$ S b 1.238	504 $15^h 40^m$ M a 1.029	483 $16^h 00^m$ S a 1.401	871 $16^h 20^m$ S b 1.000
					19 12 22 28 18 22	16 20 14 16 11 8	9 13 32 18 6 14	5 3 3 6 4 5
					48 31 31 36 23 51	12 18 19 19 12 18	13 19 29 21 9 15	7 5 4 5 1 7
					26 21 22 18 33 27	26 18 12 11 21 14	18 25 19 32 27 21	4 1 0 0 3 4
					17 14 9 18 25 39	14 11 16 8 11 9	45 36 45 25 22 11	8 4 3 5 7 3
10 12 7 27 32 8	12 14 9 7 15 7	26 24 48 49 64 11	4 3 1 6 6 5					
17 7 12 16 15 15	20 12 17 17 12 10	13 25 46 26 17 7	5 5 5 3 3 2					
850 $16^h 40^m$ S b 1.000					891 $17^h 00^m$ S b 1.000	1615 $17^h 20^m$ S h 1.047	534 $17^h 40^m$ S a 0.914	505 $18^h 00^m$ S a 0.914
					9 3 11 8 9 8	3 2 1 8 3 9	1 1 1 1 0 0	0 0 0 0 0 0
					7 4 6 9 6 5	6 5 2 5 3 1	0 1 0 1 0 1	0 0 0 0 0 0
					3 5 4 4 2 4	2 5 1 2 2 4	0 0 0 1 1 0	0 0 0 0 0 0
					4 3 1 7 2 4	5 3 0 4 1 0	0 1 0 0 2 1	0 0 0 0 0 0
8 13 3 5 7 6	1 1 1 2 5 4	0 0 1 0 3 1	0 0 3 0 0 0					
5 13 5 6 3 3	1 2 1 1 3 1	3 2 0 1 1 1	0 0 0 0 0 0					

$\delta = -10^\circ$									
1529 12 ^h 00 ^m S h 0.740		827 12 ^h 20 ^m S b 1.144		1145 12 ^h 40 ^m S e 0.781		453 13 ^h 00 ^m W a 0.924			
63 89 79 44 60 47	59 48 57 54 65 33	42 79 69 84 84 60	33 55 47 68 51 33	63 59 34 41 49 44	59 76 56 30 29 43	85 98 61 93 61 64	53 45 56 48 49 75		
31 32 36 52 58 35	31 51 37 38 36 24	125 70 68 52 82 37	62 36 39 64 69 88	44 37 22 35 41 52	62 52 58 47 31 34	81 49 49 126 96 58	62 42 34 54 52 63		
53 37 29 34 51 40	45 52 34 48 50 30	88 75 104 72 46 54	43 40 54 48 60 93	44 40 52 51 57 39	26 32 41 54 33 18	109 60 71 71 39 44	66 31 47 69 108 85		
1231 13 ^h 20 ^m S f 1.090		463 13 ^h 40 ^m S a 0.973		1207 14 ^h 00 ^m W e 0.937		1584 14 ^h 20 ^m S h 1.037		828 14 ^h 40 ^m S b 1.022	
38 39 33 30 27 33	55 57 47 37 31 29	82 84 45 51 53 46	21 37 29 32 27 24	70 37 29 44 39 42	37 89 62 43 29 27	40 36 18 43 19 22	46 49 59 42 56 41	56 41 28 32 31 47	14 42 39 22 37 45
60 46 25 26 32 39	14 62 89 57 65 50	58 40 98 73 44 52	35 32 21 34 30 39	67 54 55 34 32 25	49 71 74 38 31 28	21 10 32 28 21 36	25 20 16 24 18 20	53 48 66 55 39 35	84 67 40 64 58 78
	61 32 45 39 45 41	43 45 24 38 81 81	17 24 18 18 7 22		50 70 62 127 85 66	19 12 19 16 25 28	42 26 33 35 22 17		81 32 45 39 45 41
					43 45 24 38 81 81	36 13 23 21 13 16	17 24 18 18 7 22		
832 15 ^h 00 ^m S b 1.273		454 15 ^h 20 ^m S a 0.912		498 15 ^h 40 ^m M a 1.163		457* 16 ^h 00 ^m S a 0.652		869 16 ^h 20 ^m S b 1.017	
33 24 12 24 12 16	12 22 31 49 29 38	39 41 24 8 8 10	14 14 18 29 15 10	24 22 18 43 25 36	8 42 35 20 26 29	22 28 41 25 38 23	23 23 20 26 17 11	34 21 28 13 25 26	32 16 30 65 30 41
28 29 22 22 16 21	28 30 30 55 34 39	19 18 13 18 25 14	23 25 18 15 13 14	34 21 28 13 25 26	32 34 30 26 40 18	19 25 14 23 33 30	25 12 12 16 16 10	26 29 22 22 16 21	28 30 30 55 34 39
33 26 29 16 24 27	18 36 20 30 31 39	12 14 35 31 25 9	24 16 16 11 14 17	9 11 17 21 17 13	9 19 33 17 14 17	26 21 27 28 33 22	16 14 11 11 11 9		18 36 20 30 31 39
									20 24 20 21 18 6
878 16 ^h 40 ^m S b 1.000		829 17 ^h 00 ^m S b 1.000		1623 17 ^h 20 ^m W h 1.031		1246 17 ^h 40 ^m S f 1.084		499 18 ^h 00 ^m S a 0.914	
5 13 16 7 4 5	0 1 1 0 4 5	0 2 1 0 0 3	1 0 0 0 0 0	15 9 11 5 12 8	3 3 11 4 7 6	2 1 0 0 0 1	0 0 0 1 0 0	0 1 1 0 0 0	0 1 1 0 4 5
6 6 1 3 4 1	13 8 2 6 3 2	2 0 0 1 0 2	0 0 0 0 1 0	4 2 0 1 7 7	5 9 5 3 5 0	1 0 0 1 0 1	0 0 0 0 0 0	0 0 0 0 0 0	13 8 2 6 3 2
4 1 6 4 4 2	8 6 3 13 8 0	0 0 0 0 0 0	0 0 0 0 1 0	4 1 6 4 4 2	8 6 3 13 8 0	0 0 0 0 0 0	0 0 0 0 0 0	0 0 0 0 0 0	5 9 5 3 5 0
2 7 10 4 2 1	2 4 1 7 1 4	0 1 0 1 0 1	0 0 0 0 0 0			1 0 0 0 0 0	0 0 0 0 0 0	0 0 0 0 0 0	2 4 1 7 1 4
		0 1 0 1 0 1	1 0 0 0 0 0			1 0 0 0 0 0	0 0 0 0 0 0	0 0 0 0 0 0	
$\delta = -5^\circ$									
451* 12 ^h 00 ^m W a 1.581		834 12 ^h 20 ^m S b 1.012		439 12 ^h 40 ^m S a 0.848		447 13 ^h 00 ^m S a 0.924			
32 23 35 27 30 55	35 46 39 38 45 28	54 83 65 83 44 39	53 61 118 69 55 46	33 29 28 32 26 40	55 41 44 33 65 42	67 93 58 77 76 71	65 60 76 119 47 51		
31 49 46 26 19 50	62 43 38 80 77 50	89 117 96 144 104 68	61 68 48 97 62 63	94 39 39 27 41 53	57 50 48 52 55 100	62 109 106 106 59 69	35 68 58 62 42 48		
55 34 55 48 32 36	55 42 54 60 119 79	81 86 92 75 59 48	45 62 50 58 44 68	25 34 34 14 20 25	73 52 59 49 63 41	47 71 71 75 75 50	33 56 39 68 54 31		
1211 13 ^h 20 ^m W e 0.977		1181 13 ^h 40 ^m W e 0.796		1203 14 ^h 00 ^m W e 0.732		849 14 ^h 20 ^m S b 1.322		822 14 ^h 40 ^m S b 0.804	
49 49 51 41 33 45	56 34 35 44 35 58	53 48 21 63 43 49	45 50 59 30 33 31	43 67 85 56 47 50	37 27 24 22 61 46	14 43 15 26 20 33	76 106 55 47 35 36	43 47 41 50 50 45	34 39 40 53 39 39
35 39 58 37 51 32	56 71 54 58 55 31	77 51 52 44 31 37	46 51 25 28 54 19	39 34 34 39 27 32	43 91 47 46 36 32	36 26 9 39 24 35	48 48 46 32 34 24	32 42 48 29 40 38	49 63 53 47 40 38
442 15 ^h 00 ^m S a 0.979		474 15 ^h 20 ^m S a 0.685		508 15 ^h 40 ^m M a 0.846		464 16 ^h 00 ^m M a 1.390		872 16 ^h 20 ^m S b 1.056	
23 32 36 24 24 23	21 28 19 36 30 30	16 28 42 32 40 30	20 18 11 17 15 17	38 40 41 34 30 37	34 30 43 32 30 78	12 39 8 15 4 7	15 14 4 19 11 7	41 65 43 32 32 54	47 43 29 47 30 70
38 40 41 34 30 37	47 43 29 47 30 70	45 37 30 27 40 28	11 4 7 9 5 9	38 43 33 39 51 28	33 38 42 45 50 62	15 12 26 14 20 15	7 10 10 7 7 7	36 50 41 52 26 13	38 39 59 54 52 57
						0 21 13 18 7 11	13 15 12 9 9 2		
820 16 ^h 40 ^m S b 1.583		823 17 ^h 00 ^m S b 1.233		839 17 ^h 20 ^m S b 1.000		1274 17 ^h 40 ^m S f 1.084		509 18 ^h 00 ^m S a 0.914	
17 15 10 6 4 11	3 6 4 12 3 12	3 3 1 0 1 0	0 0 0 0 0 1	7 9 7 7 4 8	3 4 3 5 6 9	0 1 1 1 0 1	0 0 0 0 0 0	10 12 8 1 6 10	2 4 6 5 3 10
8 8 3 5 10 3	6 7 4 6 6 5	0 1 1 0 1 5	0 1 0 1 0 1	4 9 1 11 7 4	4 3 5 4 11 0	0 0 1 0 0 0	0 1 0 0 0 0	9 15 5 13 6 5	2 6 5 4 5 3
		1 1 0 4 4 1	0 0 0 0 0 0			0 0 0 0 0 0	0 0 0 0 0 0		

					792 12 ^h 00 ^m					821 12 ^h 20 ^m					441 12 ^h 40 ^m					444 13 ^h 00 ^m									
					S b 0.769					W b 0.793					S a 1.053					S a 1.003									
δ = 0°					71	82	137	113	84	55	74	68	81	50	55	62	29	47	71	63	62	49	45	52	43	47	58	26	
	61	72	101	59	78	52	55	45	49	87	47	50	52	53	125	91	54	53	80	53	47	57	44	41					
	71	84	89	102	85	74	88	50	30	49	53	64	62	102	121	73	41	73	62	47	50	48	40	55					
	99	78	73	119	120	76	42	73	27	56	81	53	67	93	92	48	68	39	96	70	67	41	47	44					
	54	66	77	81	88	90	96	69	38	61	65	66	103	150	100	75	43	44	42	70	60	97	79	61					
	56	49	66	58	59	55	63	68	65	64	45	58	64	66	51	61	33	26	45	66	124	94	48	37					
					480 13 ^h 20 ^m					1234 13 ^h 40 ^m					1247 14 ^h 00 ^m					793 14 ^h 20 ^m					825 14 ^h 40 ^m				
					S a 0.714					W f 1.534					S f 0.990					S b 0.820					S b 1.331				
84	62	59	47	53	57	60	25	48	59	31	28	43	26	29	28	18	59	92	50	64	62	109	56	24	27	27	33	36	44
108	110	117	74	76	74	32	38	24	24	32	39	74	36	36	43	26	35	88	79	74	74	100	80	25	22	39	27	37	49
80	107	131	82	80	74	30	26	39	28	45	26	69	48	34	28	27	41	91	91	61	48	79	68	38	38	27	35	38	52
91	72	99	172	126	108	21	22	29	41	33	20	82	82	67	23	43	29	65	73	75	74	101	97	36	42	25	35	55	35
121	98	76	87	66	51	27	37	22	36	32	72	41	59	37	41	30	37	87	110	63	46	59	36	44	40	32	41	61	43
59	61	62	57	57	35	35	23	19	21	16	32	29	41	28	55	27	38	44	51	45	52	47	25	19	30	42	21	23	24
					492 15 ^h 00 ^m					445 15 ^h 20 ^m					481 15 ^h 40 ^m					491 16 ^h 00 ^m					1248 16 ^h 20 ^m				
					S a 0.875					S a 0.956					M a 1.500					S a 0.676					S f 1.169				
63	47	43	59	40	30	30	62	55	82	68	46	16	20	25	33	40	27	36	60	49	60	41	20	16	24	24	17	19	22
97	83	58	55	52	47	60	75	62	66	67	67	7	12	12	26	14	28	51	67	21	24	22	20	15	8	16	24	25	16
74	65	40	49	35	46	87	61	34	34	51	48	14	38	24	23	7	48	71	66	46	47	33	50	27	19	15	32	22	38
46	60	37	30	54	51	32	42	28	37	51	31	18	39	33	30	29	41	44	55	62	52	40	25	27	19	24	12	11	20
40	71	46	44	52	55	31	30	21	22	30	18	10	7	9	22	15	23	57	37	36	30	49	16	27	12	16	21	17	28
20	25	37	27	17	20	20	16	14	26	38	26	5	20	17	16	24	16	31	50	28	15	11	4	19	10	13	20	15	16
					876 16 ^h 40 ^m					836 17 ^h 00 ^m					521 17 ^h 20 ^m					1275 17 ^h 40 ^m					514 18 ^h 00 ^m				
					S b 0.733					S b 0.891					S a 0.914					S f 1.084					S a 0.914				
21	14	12	12	9	15	22	26	34	31	23	26	2	1	5	6	6	3	2	0	1	2	6	3	0	0	3	1	3	0
20	15	6	24	13	11	25	20	18	35	36	18	2	2	5	0	4	6	3	2	0	1	3	0	1	1	1	1	2	1
24	16	10	17	21	19	16	9	13	13	14	13	0	3	8	7	2	6	1	0	0	6	0	0	0	0	0	0	2	2
30	27	33	16	22	27	11	6	2	7	6	13	2	3	7	14	6	9	0	0	0	0	2	1	1	0	1	2	2	1
33	30	40	20	32	34	5	8	7	19	41	8	3	6	7	18	7	2	2	3	4	1	2	0	0	0	1	0	1	1
30	25	23	16	22	29	4	8	12	8	5	16	2	4	0	2	1	2	1	3	1	0	1	0	0	0	0	0	1	0
					758 12 ^h 00 ^m					824* 12 ^h 20 ^m					818 12 ^h 40 ^m					467 13 ^h 00 ^m									
					W b 1.066					S b 1.217					W b 0.792					S a 0.814									
δ = +5°					58	37	42	40	42	76	41	63	70	54	50	39	63	81	48	45	54	72	87	79	101	82	58	51	
	89	67	43	54	56	74	95	84	65	91	63	64	83	53	49	118	94	98	93	69	97	64	62	64					
	80	62	44	56	89	100	90	66	76	127	121	65	88	97	53	62	71	119	136	64	75	89	78	84					
	49	40	94	39	73	85	60	41	105	68	93	47	106	75	69	93	101	98	101	71	103	66	66	105					
	46	36	40	61	47	60	87	72	78	69	93	53	72	49	90	104	63	105	82	83	96	61	94	53					
	45	51	94	73	52	36	43	48	59	36	38	41	53	55	98	83	83	76	52	61	51	39	61	27					
					1232 13 ^h 20 ^m					1236 13 ^h 40 ^m					1216 14 ^h 00 ^m					819 14 ^h 20 ^m					835 14 ^h 40 ^m				
					W f 1.229					S f 0.911					S e 1.112					S b 1.106					S b 1.021				
39	33	25	37	89	27	65	58	65	50	34	53	40	55	61	41	56	46	45	55	38	41	51	41	41	50	48	41	42	54
34	25	47	40	41	55	50	53	47	54	56	28	61	88	89	54	68	38	48	66	93	75	57	59	46	42	35	52	65	54
50	28	35	50	55	76	112	64	40	54	29	40	101	76	48	58	68	95	96	58	76	73	115	78	82	41	28	52	55	60
29	22	24	35	44	52	50	63	84	86	48	36	24	34	39	36	54	30	85	74	71	57	74	38	48	46	69	52	56	61
31	26	34	43	34	41	43	69	80	71	64	40	52	39	46	47	48	27	79	99	55	37	60	67	89	55	77	122	84	87
71	46	37	41	37	39	79	39	65	106	65	49	42	18	31	25	18	55	58	47	54	63	90	45	33	31	36	35	38	48
					817 15 ^h 00 ^m					448 15 ^h 20 ^m					815* 15 ^h 40 ^m					1182 16 ^h 00 ^m					1217 16 ^h 20 ^m				
					S b 0.811					S a 1.151					S b 0.734					S e 0.884					S e 0.966				
165	126	90	43	27	33	48	66	96	90	113	83	32	41	75	92	63	77	11	19	14	19	18	13	25	39	29	19	15	14
198	115	63	44	67	64	47	63	69	85	82	112	62	66	50	85	54	72	29	41	20	48	65	47	24	36	40	27	26	17
243	108	119	81	95	104	63	85	91	114	124	161	45	39	68	59	55	91	33	35	50	42	26	33	27	32	32	27	33	29
256	96	59	52	47	52	78	118	123	213	199	177	53	45	69	55	62	86	48	33	30	27	33	41	25	17	36	16	16	31
148	123	63	61	70	93	55	96	56	111	87	75	24	38	48	95	44	61	31	55	31	28	26	17	23	37	38	24	14	15
94	59	55	49	54	24	31	51	55	68	51	44	23	25	41	48	53	34	25	40	33	57	29	17	19	25	36	19	21	16
					1585 16 ^h 40 ^m					1229 17 ^h 00 ^m					1227 17 ^h 20 ^m					842 17 ^h 40 ^m					913 18 ^h 00 ^m				
					S h 1.146					S f 1.050					S f 1.099					S b 1.060					S b 1.000				
12	13	11	23	27	20	7	8	8	12	7	16	8	9	6	7	15	4	4	10	9	9	6	10	4	2	3	2	2	1
10	28	18	18	33	15	12	8	9	11	12	13	15	15	13	12	21	20	10	7	5	7	15	18	2	6	1	3	1	6
12	11	11	19	18	16	15	6	13	7	14	10	10	6	11	7	5	11	7	5	10	5	14	6	2	2	2	2	2	3
28	15	16	17	11	13	11	17	15	7	12	26	3	3	5	7	6	10	4	4	8	10	5	2	3	4	4	1	0	2
20	18	13	16	6	14	14	13	14	16	11	16	5	10	3	3	0	3	3	4	3	5	1	2	2	0	1	3	4	0
12	13	7	9	12	10	11	9	14	13	17	11	4	4	2	6	5	4	0	1	4	2	6	5	5	1	4	4	3	3

$\delta = +10^\circ$																							
1149 12 ^h 00 ^m S e 1.016			1140 12 ^h 20 ^m S e 0.814			831 12 ^h 40 ^m S b 1.118			471 13 ^h 00 ^m W a 0.742														
60	69	47	42	41	79	115	130	111	125	89	69	33	31	80	64	55	57	92	78	78	69	37	47
65	110	66	51	123	73	108	129	64	68	63	71	27	53	61	61	65	72	114	83	115	59	59	55
71	98	99	93	85	51	122	108	103	75	78	70	52	45	69	70	81	80	63	104	70	56	68	92
75	46	49	48	61	65	104	153	113	82	71	92	67	43	70	73	71	89	101	176	128	101	74	86
51	46	37	37	29	58	75	136	99	136	102	69	64	61	79	51	62	44	106	118	122	89	105	113
68	47	50	39	42	49	55	73	96	65	62	58	47	71	51	46	57	35	63	58	77	69	39	44
1508 13 ^h 20 ^m S h 1.092			1238 13 ^h 40 ^m W f 1.083			1249 14 ^h 00 ^m S f 0.954			1597 14 ^h 20 ^m S h 0.882			1592 14 ^h 40 ^m S h 1.078											
47	103	48	52	52	43	59	59	47	46	32	50	97	93	88	69	68	65	70	69	42	32	46	50
95	132	92	122	61	59	57	51	51	58	57	78	85	92	68	47	68	60	73	106	61	40	62	86
104	70	52	62	53	50	48	34	37	59	64	78	49	100	84	75	53	47	86	54	31	31	43	29
69	64	39	49	79	54	83	63	40	58	45	54	60	66	117	71	42	78	98	39	59	72	75	52
48	66	76	62	73	45	61	59	40	31	53	36	76	81	37	60	48	37	67	62	39	52	157	91
55	40	30	40	77	38	79	70	75	57	40	55	54	71	52	34	60	34	87	113	56	67	68	67
838 15 ^h 00 ^m S b 0.912			472 15 ^h 20 ^m S a 1.069			1255 15 ^h 40 ^m S f 1.069			1235 16 ^h 00 ^m S f 1.448			1224 16 ^h 20 ^m S f 0.916											
47	56	48	69	66	51	27	26	28	34	35	24	44	46	16	35	49	25	22	33	23	23	34	31
62	58	72	72	61	64	31	42	51	34	40	60	25	40	48	28	31	27	25	27	23	19	42	22
47	83	82	58	41	75	57	52	63	43	56	36	47	45	41	36	47	46	21	17	12	33	16	39
59	86	93	66	127	59	46	41	63	42	33	46	65	65	50	19	40	27	18	16	18	21	27	36
80	155	130	55	48	47	51	77	133	120	73	48	65	72	93	60	50	40	15	30	29	19	12	17
153	137	71	32	22	31	53	74	87	95	112	86	17	24	41	58	31	47	8	10	9	10	8	6
1270 16 ^h 40 ^m S f 1.024			881 17 ^h 00 ^m S b 1.469			524 17 ^h 20 ^m S a 1.112			1621 17 ^h 40 ^m S h 1.060			915 18 ^h 00 ^m S b 1.168											
20	20	19	23	20	23	8	4	8	9	9	7	9	6	10	4	6	4	4	6	7	6	11	5
24	24	38	53	25	30	2	11	10	9	13	9	4	15	4	8	4	4	6	7	8	9	10	1
18	22	17	18	21	14	6	9	13	11	8	12	4	9	4	14	12	6	6	4	8	8	9	5
10	18	26	30	19	19	8	18	15	10	6	4	12	6	4	14	14	13	4	6	10	17	5	4
11	21	21	16	18	23	6	2	7	8	7	4	8	14	19	29	20	6	1	2	9	6	7	5
15	9	12	17	26	13	4	7	8	7	5	6	6	8	8	9	17	4	7	6	13	10	6	6
$\delta = +15^\circ$																							
1132 12 ^h 00 ^m S e 0.752			1136 12 ^h 20 ^m S e 0.831			449 12 ^h 40 ^m S a 1.106			473 13 ^h 00 ^m W a 0.890														
73	59	65	56	55	55	64	75	89	67	56	43	37	53	47	68	66	40	67	52	54	43	38	44
79	63	54	61	60	58	116	68	86	72	78	89	30	38	56	86	128	58	63	75	38	50	32	39
120	113	63	85	70	101	62	57	54	54	62	101	29	51	33	52	76	39	85	62	56	55	29	36
157	81	75	56	44	63	49	46	53	71	98	101	45	35	41	77	67	49	101	113	59	36	48	73
150	116	86	96	111	125	65	75	91	114	101	120	39	68	50	73	57	52	78	98	53	53	57	55
77	94	60	55	81	81	107	205	135	125	92	74	33	26	64	49	44	54	53	44	59	50	30	25
1515 13 ^h 20 ^m S h 1.012			1240 13 ^h 40 ^m W f 1.148			1251 14 ^h 00 ^m W f 1.243			847** 14 ^h 20 ^m S b 1.917			1555 14 ^h 40 ^m S h 0.972											
36	68	62	60	53	46	47	56	55	52	42	25	29	50	45	44	42	60	56	78	89	52	40	26
57	77	46	75	44	58	63	56	51	44	43	37	52	57	101	63	67	46	39	96	65	25	28	40
33	38	53	68	51	45	82	46	47	62	43	22	52	91	95	98	62	76	39	60	38	29	30	24
84	73	120	70	70	57	117	61	64	62	53	70	60	70	73	61	90	90	53	47	32	29	28	26
94	83	111	56	55	57	74	50	53	32	47	85	43	64	56	65	62	82	35	46	29	28	28	12
46	91	46	65	54	43	65	66	54	55	50	59	52	65	72	41	56	55	28	23	13	12	14	14
496 15 ^h 00 ^m S a 0.951			477 15 ^h 20 ^m S a 0.815			1617 15 ^h 40 ^m S h 1.126			1237 16 ^h 00 ^m S f 1.078			1250 16 ^h 20 ^m S f 1.004											
85	88	66	51	64	127	27	36	28	21	58	71	20	34	66	37	22	18	53	63	175	53	41	25
87	85	77	88	89	136	24	45	46	28	70	67	33	42	34	49	32	19	30	64	238	105	55	25
79	50	52	50	43	66	50	52	46	55	86	73	21	34	48	27	23	23	50	87	149	97	33	16
53	62	47	51	38	74	33	45	35	55	56	48	25	37	37	33	32	25	64	68	94	42	20	16
52	53	47	53	42	46	57	40	53	56	39	51	46	25	37	48	28	24	29	51	44	30	28	30
23	42	37	61	67	33	36	39	39	55	51	29	41	40	25	35	43	22	32	41	53	40	31	42
873** 16 ^h 40 ^m S b 2.839			856 17 ^h 00 ^m W b 0.790			497 17 ^h 20 ^m S a 0.808			1273 17 ^h 40 ^m S f 1.231			1280 18 ^h 00 ^m S f 0.914											
12	5	6	3	13	3	18	9	9	18	22	23	23	13	18	12	10	16	13	23	25	31	15	12
8	13	19	7	7	11	18	19	21	17	20	26	27	20	21	17	13	19	15	18	31	18	10	11
4	8	8	18	2	12	15	14	22	29	15	15	23	20	14	9	10	14	9	24	21	16	15	11
12	4	29	9	6	11	9	24	23	17	17	24	14	22	28	9	7	7	24	23	17	13	27	10
11	9	12	21	18	25	25	28	35	26	25	29	9	16	18	17	11	12	6	14	12	7	16	7
15	6	14	9	11	13	12	14	15	17	11	16	10	14	16	11	9	10	5	11	9	3	7	6

$\delta = +20^\circ$																													
751 12 ^h 00 ^m S b 1.182				757* 12 ^h 20 ^m S b 1.113				837 12 ^h 40 ^m Wb 1.017				840 13 ^h 00 ^m S b 0.927																	
67	70	97	72	76	77	33	44	55	75	97	46	32	32	33	26	33	30	55	45	35	29	37	31						
66	48	85	98	89	119	53	29	67	55	67	49	25	28	40	42	36	42	61	65	33	37	19	19						
63	42	142	76	36	106	57	42	76	61	63	53	42	43	32	22	44	51	65	70	65	41	51	39						
74	51	59	45	50	50	48	52	43	77	84	53	83	58	35	66	32	48	86	85	116	103	89	52						
55	49	50	54	55	47	39	62	59	34	87	53	67	44	38	127	39	45	71	83	109	87	69	63						
48	42	43	39	41	39	39	59	61	52	51	40	36	40	54	76	63	57	50	47	43	36	38	43						
1524 13 ^h 20 ^m S h 1.179				1566 13 ^h 40 ^m S h 0.906				1577 14 ^h 00 ^m S h 0.964				1253* 14 ^h 20 ^m Wf 1.390				1591 14 ^h 40 ^m S h 0.916													
37	58	69	74	51	52	78	51	51	44	48	28	54	51	42	66	95	62	40	24	35	27	21	27	119	110	118	97	82	63
31	43	61	68	51	46	82	51	48	63	41	24	75	55	54	58	92	53	32	41	36	43	30	44	107	95	54	86	67	66
35	39	36	47	56	33	74	39	66	51	42	43	90	52	41	83	91	54	46	51	47	25	41	56	82	97	91	78	64	76
50	55	52	35	33	66	93	87	68	42	37	39	95	103	57	58	91	75	53	47	51	33	52	79	73	75	107	87	76	77
59	50	56	41	42	44	78	155	135	116	63	70	86	70	54	57	72	70	57	44	35	89	60	63	134	99	56	68	95	52
31	53	57	48	31	34	80	97	96	66	59	38	44	63	76	69	57	60	78	86	103	59	46	39	118	93	42	78	85	57
1571 15 ^h 00 ^m S h 1.200				1560 15 ^h 20 ^m S h 1.037				506 15 ^h 40 ^m S a 0.869				1239 16 ^h 00 ^m S f 1.075				1262 16 ^h 20 ^m Wf 0.989													
36	53	39	50	70	61	37	38	31	52	42	32	51	38	53	83	76	62	39	37	39	46	25	37	40	30	39	42	23	52
38	58	86	85	64	60	51	48	55	58	29	31	67	53	42	114	74	59	45	35	47	52	41	56	80	54	50	53	44	54
58	89	80	50	63	48	30	32	72	58	56	55	74	56	40	39	42	23	36	30	71	70	66	64	71	61	60	50	46	42
75	69	41	80	73	55	31	41	70	58	65	75	91	111	38	61	44	49	29	47	64	71	60	53	52	44	41	48	76	38
109	46	36	41	103	90	44	56	40	35	69	96	86	82	52	65	39	38	49	76	151	119	91	38	41	31	38	59	41	42
66	53	39	37	34	80	32	39	32	21	47	67	34	39	60	50	22	19	70	114	192	78	45	30	18	31	39	37	28	55
848 16 ^h 40 ^m Wb 1.008				519 17 ^h 00 ^m S a 0.865				833 17 ^h 20 ^m S b 1.179				1272** 17 ^h 40 ^m S f 2.310				507 18 ^h 00 ^m S a 0.940													
41	21	25	30	34	34	36	33	32	36	33	22	19	21	23	18	13	21	9	9	5	8	6	9	9	18	9	10	11	4
27	19	27	15	27	48	10	40	41	19	25	38	15	16	20	23	25	21	7	4	3	7	7	5	35	18	22	10	16	11
32	33	27	27	21	36	24	32	19	30	22	30	31	24	22	19	28	19	8	6	7	6	6	6	7	11	26	14	12	14
35	17	25	33	26	38	30	32	23	22	33	15	18	37	32	21	18	11	7	4	9	8	7	9	3	5	13	14	17	7
39	26	28	22	29	38	20	36	35	30	41	7	34	19	15	21	20	10	10	6	7	9	5	5	16	3	6	10	33	14
44	33	28	10	27	20	17	10	11	16	24	29	19	18	14	10	7	13	10	17	7	11	11	2	8	9	9	8	4	15

west-east direction. The only exception to this procedure was that Mayall counted the strips alternately from west to east and from east to west. There are 1296 separate counts recorded for each plate. The 36 counts in each square degree are combined to give the tabular values.

It is of the greatest importance to maintain a uniform standard for the identification of nebulae. This requirement is particularly difficult since by far the most numerous nebulae lie near the limit of detection. It would be possible to stop the counts somewhat above the limiting magnitude, but this procedure would necessitate estimating whether each nebula fell above or below the standard brightness. Due to the great variety of nebular forms, sizes and surface brightness, this process would be very uncertain. It was accordingly decided to count every nebula that could be identified as such with reasonable probability. It is obvious that the limiting magnitude will not be the same for all nebular types. A fairly bright but small elliptical nebula may fail to be distinguished from a star. On the other hand a large nebula of extremely low surface brightness may escape detection though its total apparent magnitude is well above the normal limit. Thus for certain types of nebulae the limit is no doubt fainter than 18.4 mag. while for

others it is brighter than this value. The value 18.4 mag. is an average limit derived from comparing our counts with those of Hubble, and it refers to the scale of magnitudes that he used.

On some plates the number of defects resembling nebulae introduces an exasperating element of uncertainty. Little can be done to avoid errors in identification beyond relying on judgment and experience. To duplicate the plates and the counts would extend the program beyond practical limits.

IV. CORRECTIONS TO THE COUNTS

In order to reduce the data to a reasonably homogeneous system, it is necessary to apply several corrections.

Off-axis correction. Due to vignetting and to some inferiority of the images at considerable distances from the optical axis there is a decrease in the number of nebulae counted with increasing distance from the center of the plate. To correct for this effect, the numbers of nebulae in each of the thirty-six square degrees were added for all the plates in Area III. The counts were again summed for all square degrees at the same distance from the plate center, and a smooth curve was drawn through these sums plotted against the distance. The reciprocals of these ordinates

are proportional to the off-axis corrections. Finally, the factor of proportionality was chosen so as to make the off-axis correction factor unity at the plate center. This "stacking" process was based on a total count in Area III of 210980 nebulae.

East-west effect. For some unexplained reason fewer nebulae are counted west of a plate center than east of it. This effect was found consistently in the counts by both Shane and Wirtanen and also in Mayall's counts which were made in alternate rows east and west. A number of suggestions to explain this puzzling phenomenon have been offered. To test any one of them adequately would require so large an amount of work that it would delay unduly the main program. It was therefore thought best to postpone an investigation of this effect.

To calculate the east-west correction, the number of nebulae in the overlapping regions of all plates were compared, except in cases where less than 30 nebulae occurred in an overlap. From a study of the plates in Area III, it was found that in a field $2\frac{1}{2}^\circ$ east of a plate center, 1.236 times as many nebulae are recorded as in the same field counted $2\frac{1}{2}^\circ$ west of the center on the overlapping plate. There is no corresponding north-south effect. This result has been checked in Area V from $\alpha = 0^h$ to $\alpha = 6^h$ and from $\delta = +20^\circ$ to $\delta = +60^\circ$. Here the east-west factor is 1.231, and again there is no certain evidence of a north-south effect.

In correcting for the east-west effect, the assumption is made that the logarithm of the correction factor varies linearly across the plate with a value of zero at the center. The factors thus derived were combined with the off-axis corrections to form a table of "field corrections." The nebular count in each square degree was accordingly multiplied by the appropriate tabular number.

TABLE II. FIELD CORRECTION FACTORS

		North					
East		1.10	1.03	1.02	1.06	1.17	1.36
		0.99	0.95	0.98	1.02	1.08	1.22
		0.94	0.94	0.98	1.02	1.07	1.16
		0.94	0.94	0.98	1.02	1.07	1.16
		0.99	0.95	0.98	1.02	1.08	1.22
		1.10	1.03	1.02	1.06	1.17	1.36

Atmospheric extinction. Corrections were made for atmospheric extinction to reduce the counts to their probable zenith values. This correction is simplified by the circumstance that all exposures were centered on the meridian, and to a sufficient approximation, therefore, the extinc-

tion factor depends only on δ . A value for the photographic extinction in the zenith of 0.30 mag., supplied by Kron, was used. The logarithm of the correction factor is accordingly equal to

$$0.60 \times 0.30 (\sec z - 1),$$

where 0.60 is the logarithm of the factor by which the number of nebulae increases per unit of limiting magnitude, on the assumption of a uniform distribution in depth, and z represents the average zenith distance of the region during the exposure. The extinction factor is read from a curve as a function of δ . The factor varies from 1.00 in the zenith to 1.53 at $\delta = -22^\circ 5'$.

Effective exposure time. Eight plates were estimated to be deficient in exposure time mostly because of haze or clouds. It was assumed that a factor of three in the exposure time corresponds to a unit change in limiting magnitude. An exposure of 100 minutes, the minimum accepted, requires that the counts be corrected by a factor of 1.26 to reduce them to the standard 120 minute exposure.

Emulsion factor. Five different emulsions were used for the plates in Area III, and as these varied slightly in sensitivity, an appropriate emulsion factor was applied in each case. The emulsion factors and the personal factors were derived together from a least-squares solution, which is discussed in detail in the next section.

Personal factor. All except five of the plates in this area were counted by the authors. Personal factors were applied to reduce Wirtanen's and Mayall's counts to the standard of the senior

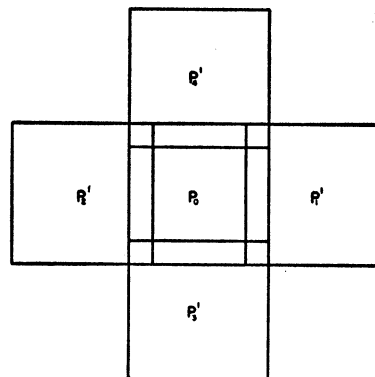


Figure 1. Plate notation.

author. The following method was used in determining this factor and the emulsion factor.

To explain the notation reference is made to Figure 1, which represents a particular photograph with its four overlapping plates. The over-

lap regions are the four long rectangles including the corner squares, so that each corner is included twice.

Let

ν_m^0 = the true number of nebulae in overlap m to the standard limiting magnitude,

ν_m, ν_m' = numbers of nebulae counted in m on plates P_0 and P_m' , respectively,

$\alpha_m = \alpha_m'$ = average off-axis correction for region m on P_0 and P_m' , respectively,

q = east-west factor,

$\beta_m = \beta_m'$ = average extinction correction for region m ,

i_0, i_m' = exposure deficiency factors for P_0 and P_m' , respectively,

ϵ_0, ϵ_m' = emulsion factors for P_0 and P_m' , respectively,

p_0, p_m' = personal factors for P_0 and P_m' , respectively.

$$\rho_m = \frac{\nu_m'}{\nu_m}$$

Then

$$\nu_1 = \frac{\nu_1^0}{\alpha_1 \beta_1 i_0 \epsilon_0 p_0 q},$$

$$\nu_1' = \frac{\nu_1^0 q}{\alpha_1' \beta_1' i_1' \epsilon_1' p_1'}$$

Whence

$$\rho_1 = \frac{i_0 \epsilon_0 p_0 q^2}{i_1' \epsilon_1' p_1'}$$

or

$$\begin{aligned} \log \rho_1 + \log i_1' - \log i_0 - \log q^2 \\ = \log \epsilon_0 - \log \epsilon_1' + \log p_0 - \log p_1' \end{aligned}$$

The corresponding equation for $m = 2$ has the same form except that q^2 is replaced by $1/q^2$. For $m = 3$ and $m = 4$ the q^2 term does not occur. In the solution, however, only equations for $m = 1$ and $m = 3$ are used since the observational material in $m = 2$ and $m = 4$ appears in $m = 1$ and $m = 3$ when P_2' and P_4' are adopted as P_0 . The left-hand members of the equations are known quantities. When we replace ϵ_0 and ϵ_m' by the emulsion factors appropriate to the particular plates, four unknown emulsion factors $\epsilon_a, \epsilon_e, \epsilon_f,$ and ϵ_h appear in the equations. $\epsilon_b = 1$ was adopted as standard so that $\log \epsilon_b = 0$. Similarly the personal factors p_w and p_m corresponding to Wirtanen and Mayall are unknowns,

with the factor for Shane taken as standard. The plates counted by Mayall were too few to justify inclusion in the general solutions. After the other constants were determined, p_m was calculated from the 12 equations in which it appeared. In the general solution no equation was included if either ν_m or ν_m' was less than 30.

A least-squares solution was made from the 261 resulting equations. The constants together with their probable errors are included in Table III.

TABLE III. PLATE CONSTANTS

	log	number	
ϵ_a	$-0.039 \pm .009$	0.914	Standard
ϵ_b	0.000	1.000	
ϵ_e	$-0.056 \pm .014$	0.879	
ϵ_f	$+0.035 \pm .011$	1.084	
ϵ_h	$+0.020 \pm .012$	1.047	
p_s	0.000	1.000	Standard
p_w	$-0.007 \pm .008$	0.984	
p_m	$+0.103 \pm .034$	1.268	

The ratio of the extremes of the emulsion factors is 1.234. This value corresponds to the surprisingly small range in limiting magnitude of 0.15 mag. The large value of p_m probably reflects a certain degree of conservatism in Mayall's identification of objects as nebulae.

Accidental errors. The counts on each plate are subject to a further source of error that may be treated as accidental in character. It is the compounded effect of seeing, night-to-night fluctuations in atmospheric transmission, variation of plate sensitivity within a given emulsion, non-uniformity in processing the plates, and irregular changes in the personal counting factors. In addition to these sources of variation, there may be others of a more obscure nature. The best that can be done to determine the "accidental factor" is to adopt a smoothing process based on the overlaps.

Let f_1, f_m' = the accidental factors for plates P_0 and P_m' , respectively. Then for $m = 1$

$$\nu_1 = \frac{\nu_1^0}{\alpha_1 \beta_1 i_0 \epsilon_0 p_0 q} \frac{1}{f_1},$$

$$\nu_1' = \frac{\nu_1^0 q}{\alpha_1' \beta_1' i_1' \epsilon_1' p_1'} \frac{1}{f_1'}$$

whence

$$f = f_1' \rho_1 \left[\frac{i_1' \epsilon_1' p_1'}{i_0 \epsilon_0 p_0} \frac{1}{q^2} \right].$$

Let the factor in brackets be called g_1' . Expressions for g_2', g_3', g_4' are the same except that g_2' has q^2 in the numerator instead of the denominator while in g_3' and g_4' , q^2 is replaced by unity.

We thus have n equations for f of the form

$$f = f_m' \rho_m g_m',$$

where n is normally 4 but may be less if any of the plates P_m' are not used. These equations determine f in terms of f' . In addition we should use the equation $f = 1$ to give appropriate weight to P_0 . If we multiply the $n + 1$ equations together we get

$$f^{n+1} = \prod_n f_m' \rho_m g_m'.$$

The smoothing process depends on the assumption that $\prod_n f_m' = 1$. Thus

$$f = \left[\prod_n f_m' \rho_m g_m' \right]^{1/(n+1)}.$$

If the plate P_0 is of such low weight that its accidental factor, f , should be determined solely from its neighbors, we replace the exponent $1/(n + 1)$ by $1/n$, i.e., we omit the equation $f = 1$. In Area III there were seven plates that for one reason or another were omitted in calculating the constants and the f 's. All but one were strongly deficient in numbers of nebulae as compared with the numbers in their overlaps. In most cases this effect was verified by an examination of the star images. A single plate ($\alpha = 14^{\text{h}}20^{\text{m}}$, $\delta = -20^\circ$) showed a great excess of nebulae. The reason is not known but it was thought desirable to omit this plate in determining the constants.

No overlap was used in calculating f if ρ_m depended on ν_m or ν_m' less than 30. In and near the zone of avoidance this was the usual situation, so that for many plates, f was taken equal to unity.

A study of the f factors reveals that their logs are distributed about zero in an approximately normal manner with a slight excess of large and small values. The probable departure of $\log f$ from zero is ± 0.055 .

Let us designate by F the complete plate factor for P_0 . This quantity equals f multiplied by the exposure, emulsion and personal factors.

Thus

$$F = f i_0 \epsilon_0 p.$$

The value of F calculated for each plate is included in Table I.

The reduction of the counts requires first that the field and extinction factors shall be applied for each square degree on a plate, and that these

values shall then be multiplied by the appropriate F . After these corrections have been applied to the counts, the material is ready for discussion.

V. THE PROBABLE ERRORS

The comparison of corrected counts in the same square degree on overlapping plates provides material for calculating the probable errors. Only the northwest quarter of Area III was used since it contains sufficient data for a solution, and it is the region of greatest nebular density. The logarithm of the ratio of counts in overlapping regions was formed from 510 comparisons. The resulting probable error in the logarithm of the nebular count per square degree is 0.054 which corresponds to ± 12.5 per cent of the number of nebulae. The probable error in the logarithm applies to counts in the more populous area, and it should obviously be larger in areas of low nebular density. The distribution of residuals closely follows a normal error curve. An application of the χ^2 test showed that the probability of a poorer fit than that obtained is 0.40.

The errors arise from several sources, the most important of which appear to be:

1. The plate factors, F , are not determined with complete accuracy because they depend on a smoothing process that reduces but does not eliminate the individual plate errors.
2. The limiting magnitude is not necessarily constant over a given plate but varies with any non-uniformity of emulsion sensitivity and with dark-room processing.
3. Some nebulae may be overlooked in counting while certain plate defects may be recorded as nebulae.
4. In counting near the limit of detectability the observer cannot maintain a uniform standard of identification.

If all the discrepancies among the counts were assigned to variations in emulsion sensitivity alone, they could be accounted for by a probable error in the sensitivity of only 0.09 mag. A variable plate sensitivity cannot, of course, bear the entire responsibility, and its effect may well be equaled or exceeded by one or more of the other sources of error. If this conjecture is correct, the observations indicate a rather remarkable uniformity of emulsion coating over a one-degree border around the large plates.

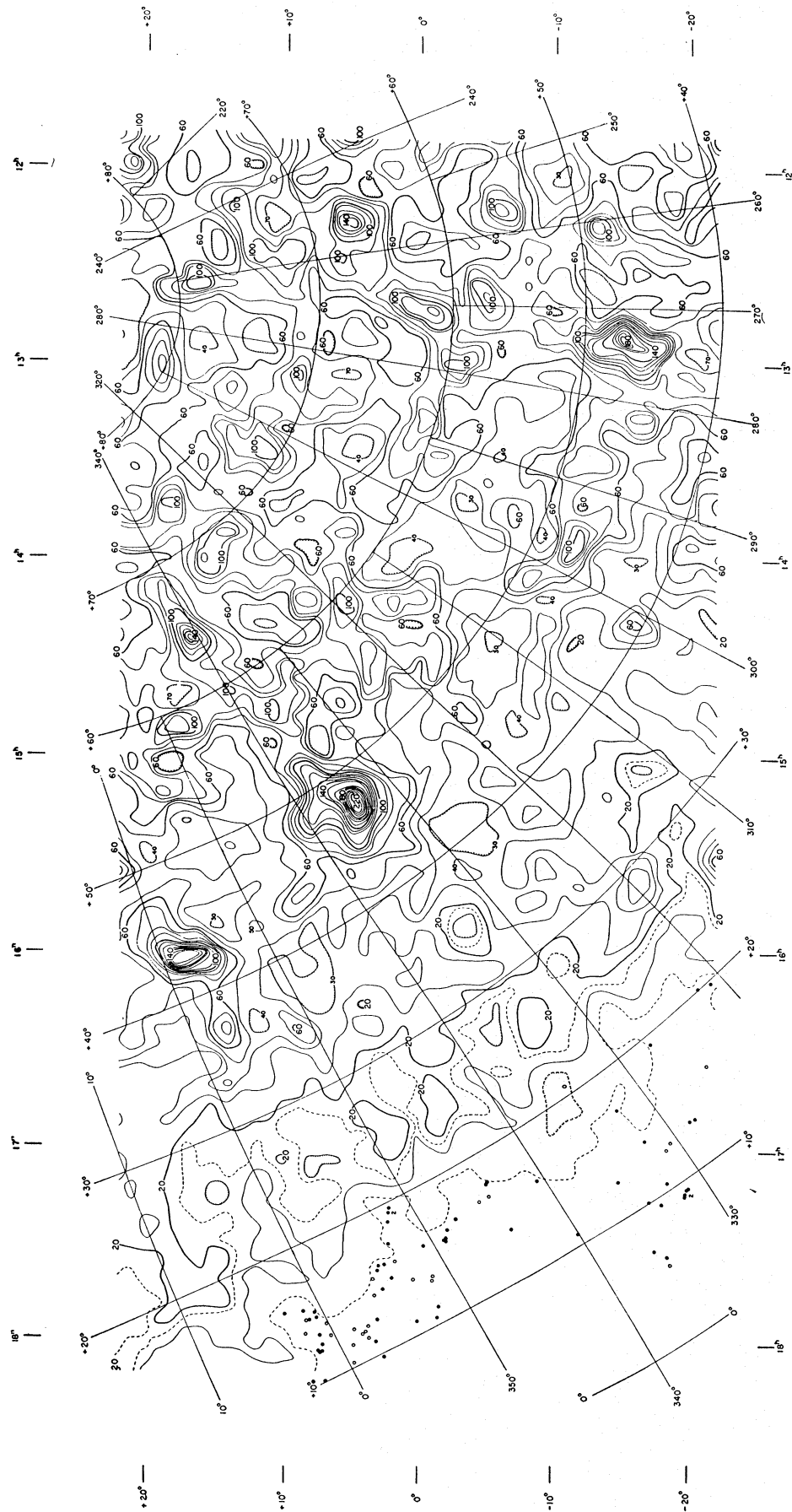


Figure 2. Equal surface density contours for nebulae in Area III, based on smoothed counts by 1° squares.

VI. THE CONTOUR MAP

The general features of the nebular distribution are probably best portrayed by means of a contour map showing curves of equal surface density. In drawing the contours it is not feasible to use the individual reduced counts by square degrees. For one reason, the variation in numbers of nebulae between adjacent square degrees is so irregular that excessively complicated contours would be required. Moreover, the probable errors of the counts are of such size that in many cases this complicated detail would be misleading. It was therefore decided to form running means of four square degrees and to base the map on these values. Every combination of four square degrees having a common corner was averaged, and the results were entered on a chart at the position of the corner. The contour map, Figure 2, was drawn from these data. The contour interval is ten nebulae per square degree, with the contours 20, 60, 100, 140, etc. drawn in heavy lines. In addition the contours representing 5 and 15 nebulae per square degree are indicated by broken lines. Completely enclosed areas of lower density are shown by hachures on the lowest contours of such areas. The process of smoothing by fours obviously conceals some detail and suppresses the relief to a certain extent. For example, if we consider the three great clouds of nebulae that lie between galactic latitudes $b = +40^\circ$ and $+50^\circ$, the maximum contours are 180, 220, and 160, whereas the most populous square degrees contain 244, 272, and 258 nebulae, respectively. The two strongly deficient areas at galactic longitude $l = 212^\circ$, $b = +34^\circ$ and at $l = 333^\circ$, $b = +35^\circ$ each have minimum contours of 10, whereas the minimum numbers of nebulae are 7 and 2, respectively. The actual relief is thus greater than is indicated by the map.

Individual nebulae on the low density side of the number 5 contour are indicated by small circles. The open circles represent nebulae that have a strong appearance of reality but were observed on only one plate. Nebulae represented by the filled circles were verified on at least one additional plate. Nevertheless the identities of many of these objects are open to question. In one case a Crossley photograph and a spectrogram by Gibson Reaves revealed that an apparent extragalactic object is, in fact, a small planetary resembling the Owl nebula. A second object highly plausible as a nebula proved to be stellar on another Crossley photograph by Reaves. It is probably a carbon star in which the strong blue-green region of the spectrum is sufficiently out of focus on the astrograph plates to give it the appearance of a nebula. The objects thus plotted individually should not be regarded definitely as extragalactic in nature, without further confirmation.

VII. DISTRIBUTION IN LATITUDE

The contour map shows clearly the well known correlation between the number of nebulae and the galactic latitude. From his counts Hubble derived the following expression for this relationship:

$$\log N_H = 2.115 - 0.15 \csc b,$$

where N_H is the number of nebulae and b is the galactic latitude.⁶ This equation is appropriate to a uniform layer of absorbing material lying symmetrically about the galactic equator and extending to infinity in all directions parallel to that plane. The irregularities in the distribution of galactic absorbing matter should produce departures from this simple formula, but it serves to delineate the obscuration approximately.

TABLE IV. VARIATION OF NUMBER OF NEBULAE WITH LATITUDE

Long. Interval	No. of Values of N	A	B	$\log N_H - \log N$	No. of Points
240°-260°	10	2.17	-0.29 ± .11 (p.e.)	+0.10	6
260-280	16	1.78	+0.05 ± .07	+0.05	14
280-300	20	2.12	-0.29 ± .07	+0.07	41
300-320	24	2.25	-0.43 ± .03	+0.16	18
320-340	23	2.42	-0.51 ± .03	+0.13	18
340-360	23	2.46	-0.55 ± .03	+0.15	15
0-20	5	2.46	-0.54 ± .16	+0.52	3

The more complete data now available justify separate solutions, by 20° longitude intervals, of the equation

$$\log N = A - B \csc b,$$

where N represents the average of the corrected numbers of nebulae per square degree for each plate whose center lies within a given longitude interval. The constants, A and B , were determined by least-squares solutions for seven longi-

tude intervals in Area III. Values of N corresponding to $b < +25^\circ$ and a few values of N in the more conspicuous clouds were omitted from the solution. The results are included in Table IV.

The first four columns are self explanatory. The fifth column contains the means of the difference between the logarithms of Hubble's counts⁶ corrected for quality, $\log N_H$, and $\log N$ as calculated from A and B . The sixth column lists the number of values of $\log N_H$ used in forming these means. It should be noted that the first three values of B are subject to considerable inaccuracy due to the small range of b , and also due to the sensitivity of B to a possible systematic error in the amount of the atmospheric extinction.

For each of the seven longitude intervals, $\log N$ was plotted as a function of $\csc b$ (Figures 3 to 9). The straight line corresponding to the constants A and B is drawn for each figure. The points used in the solution are indicated by circles. Those that correspond to positions in large clouds of nebulae are represented by dots, and Hubble's values are shown by crosses. One of Hubble's points that coincides with a large cloud is omitted.

It is evident that in Area III the constant B is much larger than that derived by Hubble in the more extensive area covered by his survey. Since Area III includes part of the galactic bulge where the strong absorption persists to a considerable distance from the galactic equator, we would anticipate a larger absolute value of B than the 0.15 Hubble determined. However, the distribution of the points representing his observations in Area III suggests that a solution from them would yield a value of B even larger than ours.

An average value of B suitable for reducing the counts in Area III to a standard galactic absorption at the pole may be calculated from the data in Table IV. For this purpose it is recognized that the variation in B with longitude is for the most part real and does not result from accidental effects. Therefore the best average value is the unweighted mean. Since the corrections would ordinarily be used only in intermediate or higher latitudes, and since Area III does not include the longitude range $l = 0^\circ - 20^\circ$ in these latitudes, we omit the last value of B in Table IV. The resulting mean is $\bar{B} = -0.34$. In an earlier paper by Neyman, Scott and Shane,⁷

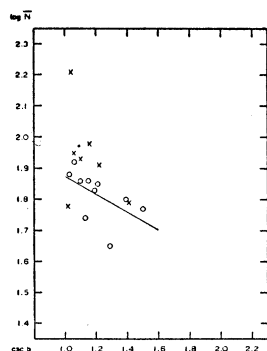


Fig.3 Long. = 240° to 260°

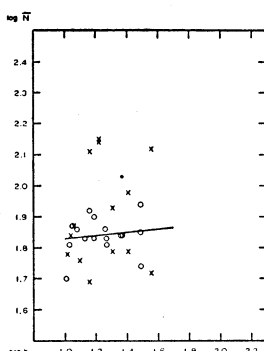


Fig.4 Long. = 260° to 280°

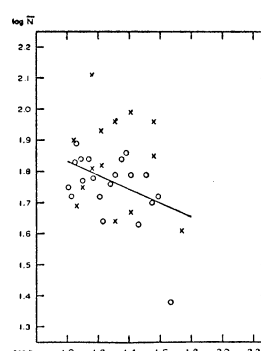


Fig.5 Long. = 280° to 300°

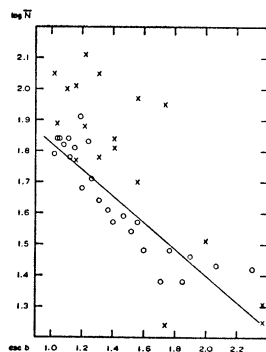


Fig.6 Long. = 300° to 320°

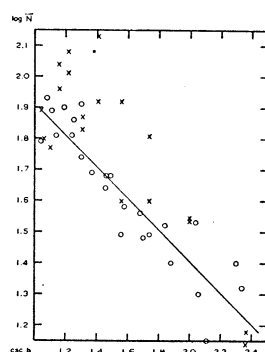


Fig.7 Long. = 320° to 340°

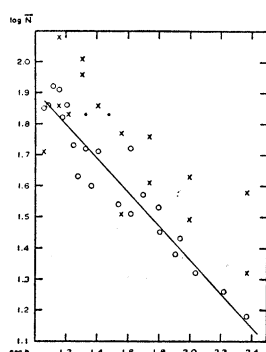


Fig.8 Long. = 340° to 360°

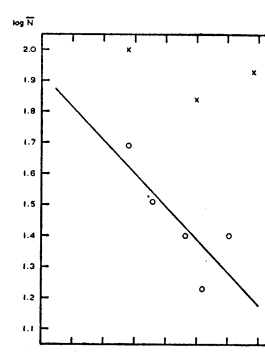


Fig.9 Long. = 0° to 20°

Figures 3-9. Relation between $\log \bar{N}$ and $\csc b$ for seven different ranges of galactic longitude.

the adopted value of \bar{B} was -0.37 , derived by including the last entry in the table.

VIII. LIMITING MAGNITUDE OF THE COUNTS

The limiting magnitude of our counts may be derived from the values of $\log N_H - \log N$ for each of the longitude intervals, listed in the fifth column of Table III. The mean of these quantities, weighted according to the number of Hubble regions, is $+0.13$. However, for comparison with our counts, $\log N_H$ must be reduced to the area unit of one square degree, and his coma factor must also be applied. When this combined correction of $+0.70$ is included, we find that the logarithm of the ratio of Hubble's counts for limiting magnitude 20.0 to our counts is $+0.83$. If a uniform average density of nebulae in depth is assumed, and if the effect of red shift is neglected, the logarithm of the number of nebulae counted should increase by 0.6 per unit of limiting magnitude. Our limiting magnitude would therefore be 1.4 mag. brighter than Hubble's, or 18.6 mag.

It is more probable that the rate of increase in the log number of nebulae should correspond to Hubble's empirical value 0.501.¹ This value yields a difference in limiting magnitude of 1.64 mag. Thus we suggest for the counts published here an approximate limiting magnitude of 18.4 mag. based on Hubble's scale. Because of uncertainties in the stellar and nebular magnitude scales near the faint end, a substantial revision of this value may be necessary at some future time.

It should again be emphasized that the assignment of a limiting magnitude to the counts does not imply that all types of nebulae are counted to this magnitude. Some nebulae can no doubt be detected beyond the stated limit while others that are somewhat brighter than the limit escape detection. The value 18.4 mag. is merely a general average for all types of nebulae.

IX. IRREGULAR GALACTIC ABSORPTION

The contour map, Figure 2, strongly suggests irregularities in the galactic absorption. Two areas markedly deficient in nebulae occur at $l = 312^\circ$, $b = +34^\circ$ and at $l = 333^\circ$, $b = +35^\circ$. These regions of deficiency probably are due to galactic absorbing clouds. Other somewhat less conspicuous regions with abnormally small numbers of nebulae are readily noted, especially in low latitudes. In several of these regions low star densities indicate that at least some of the ab-

sorbing clouds are fairly close to the sun. The behavior of the long continuous contour showing 60 nebulae per square degree is particularly striking. It seems to outline a northward extension of the area of apparent absorption between longitudes 310° and 350° , south of latitude $+40^\circ$. The extension contains several isolated deficient regions, and it reaches nearly to latitude $+70^\circ$.

In determining the true nebular distribution, it is important to know whether absorbing clouds can be observed in high latitudes. Table V con-

TABLE V. DEFICIENT REGIONS

Gal. Long.	Gal. Lat.	3 Smallest Counts		
280°	+83°	20	24	28
281	+78	28	32	34
296	+65	28	32	33
259	+62	23	26	33
330	+62	28	28	30

tains the positions of five deficient regions north of latitude $+60^\circ$ for which the nebular count falls below 40 per square degree. In this connection it should be recalled that the smoothing process applied in constructing the contour map tends to suppress the extremes and therefore the deficiencies are actually greater than are indicated by the map. The third column of Table V gives the three smallest nebular counts in each of the regions listed. Because of accidental errors it would over-emphasize the deficiencies to tabulate merely the smallest count, but the mean of two or three should give a fair idea of the minimum number of nebulae per square degree. If these areas of deficiency do represent galactic absorbing clouds, there are probably other less conspicuous clouds not so readily noted on the contour map. There are three obvious methods of testing the hypothesis that such clouds occur in high latitudes.

First, if the hypothesis is correct, nebular deficiencies in any obscured area should tend to persist when the counts are made over a wide range of limiting magnitudes. Hubble's counts are not well adapted for use in conjunction with ours in making this test, because his plates are distributed in a regular pattern over the sky and only rarely fall in strongly deficient areas. Furthermore his actual counts extend to limiting magnitude 20 only at the center of his better 100-inch reflector plates. Before the coma factor is applied, Hubble's counts average only about one magnitude fainter than ours. Thus irregularities in our results should be reflected to a considerable degree in Hubble's counts. Table VI contains the correlation coefficients for a comparison of the $\log N_H$ and $\log N$ by zones of

galactic latitude. A definite positive correlation obviously exists but the meager data do not admit of any general conclusions as to the presence of irregular absorption in high latitudes. A survey of nebulae to about 15.5 magnitude has recently been undertaken at the Lick Observatory, and at a later time it is hoped to count nebulae on plates in selected regions photographed with the 120-inch reflector. A comparison of counts to the three limiting magnitudes, 15.5, 18.4 and 21 should provide a fairly definitive test of the hypothesis of absorbing clouds in high latitudes.

TABLE VI. CORRELATION WITH HUBBLE'S COUNTS

Latitude	No. of Comparisons	Correlation Coefficient
+80° to +65°	26	+0.46
+60 to +50	32	+0.47
+45 to +40	25	+0.60
+35°	7	+0.16
+30	6	-0.08
+25	6	+0.48

A second test consists of comparing star counts with nebular counts. Any definite, positive correlation that may be found to exist would be evidence of absorption.

Finally, a possible test for absorbing clouds could be based on the colors of nebulae in the deficient areas. A systematic reddening would be strong evidence of absorption. Unfortunately the dispersion of colors among the nebulae is so great that a large number of measures of faint objects would be required. There is considerable doubt if the labor of such a program would be justified by the results.

A number of other methods of uncertain promise in this connection could be suggested, such as a search for the 21 cm radiation of neutral hydrogen in the suspected regions, the strengths of interstellar lines, and measures of the surface brightnesses of nebulae as seen through the suspected absorbing clouds. Among all the methods suggested, however, the first two, based on nebular and star counts respectively, seem to offer the best possibilities.

It is probable that interstellar clouds exist in high latitudes, and their location and measurement, or at least the determination of their statistical properties, is of great importance in a study of the true distribution of the nebulae. The investigations by Neyman, Scott and Shane are based on the simplifying assumption of no irregular absorption in high latitudes.⁷ Ambartsumian, on the other hand, derived statistical

properties of the interstellar medium from Hubble's nebular counts on the assumption that the irregularities are due to galactic absorption.⁸ The actual situation may lie somewhere between these extremes.

X. SOME STATISTICAL PROPERTIES OF THE NEBULAR DISTRIBUTION

The appearance of the contour map, Figure 2, suggests that the nebulae are not distributed at random but tend to congregate in certain areas. So many aggregations stand out prominently that one is tempted to speculate that clustering may be a predominant characteristic of nebular distribution. In considering this possibility we note that nearby clusters are relatively few in number and their members are so widely separated on the sky that they are lost among the far greater number of distant nebulae. The Virgo cluster of bright nebulae is included on the contour map, but it is quite unrecognizable because of its small number of nebulae per square degree. This cluster becomes apparent only when one takes account of apparent magnitudes. Distant clusters, on the other hand, are very numerous and therefore closely spaced on the sky, but only their few brightest members may be visible on our plates. While these nebulae contribute materially to the total counts, their distribution, when studied by square degrees, should to some extent simulate a random distribution. There is in any survey, however, an intermediate range of distance most favorable for the detection of clusters by means of counts. Thus the aggregations so prominent on the map probably are in this range, while a considerable fraction of the structureless background may come from very distant clusters.

A test of the hypothesis that all nebulae belong to clusters was made by Neyman, Scott and Shane.⁷ For this purpose the counts in the less obscured region of Area III were analyzed. The analysis depended on certain reasonable assumptions regarding the structure of clusters. The investigation showed that the main statistical properties of the distribution could be represented by the hypothesis of complete clustering. On the other hand, it is quite possible that a different model that includes an appreciable number of random nebulae could be found to represent the observations equally well.

If the nebulae are individually distributed at random we should find (1) that the numbers in neighboring square degrees are uncorrelated, and (2) that they have a Poisson distribution. Neither

of these properties is possessed by the observed distribution.

(1) Serial quasi-correlations for the counts by square degrees corresponding to the west half of the contour map, Figure 2, were calculated under the direction of Scott in connection with the paper mentioned above. After correction for observational errors and for the effects of general galactic obscuration, it was found that counts in neighboring square degrees are correlated out to a distance of four to five degrees. Since the data are fully given in the reference they are not included here. These correlations in themselves strongly suggest that some kind of clustering is a prominent feature of nebular distribution.

(2) On the basis of his counts, Hubble showed that the logarithm of the number of nebulae per counted area closely approximates a normal frequency curve with a mean $\log N = 1.925$ and a dispersion, $\sigma = 0.18$.⁶ Mayall's counts of nebulae on plates taken with the Crossley reflector likewise give an approximately normal distribution in the logarithm, with $\log \bar{N} = 1.785$ and $\sigma = 0.22$.⁹ Bok pointed out that the σ derived by Hubble is so greatly in excess of the dispersion to be expected from a random distribution that a strong degree of clustering among the nebulae is indicated.¹⁰ Hubble also suggested a small-scale clustering to explain an apparent observed decrease in σ with increasing average numbers of nebulae in the counted areas.¹

Table VII contains the results of fitting our counts as well as certain counts by Hubble and Mayall to a normal distribution curve in $\log N$. The first three columns are self-explanatory. The fourth and fifth contain, respectively, the average actual numbers of nebulae counted per standard survey area and the mean of the logarithms of their corrected values. The sixth column gives the observed dispersion. In the seventh column σ_c is the dispersion corrected for errors of observation, based on probable errors in $\log N$ for Hubble, Mayall, and Shane and Wirtanen of

0.04, 0.04 and 0.054, respectively. The eighth column, σ_r , gives the dispersion in $\log N$ on the assumption of a random distribution. The ratios in the ninth column may be regarded as a measure of the departure from randomness. In view of the contagion in distribution, these numbers should show dependence on the average size of the samples counted in each row, but the range in sample size is not great enough to make the dependence obvious. The last column, P , gives the probability that if the true distribution in $\log N$ were normal, the χ^2 test would indicate a poorer fit than was actually found.

In Table VII the Hubble counts and those by Shane and Wirtanen north of latitude $+50^\circ$, all have values of P that strongly indicate a normal distribution in $\log N$. The Mayall counts in 71 areas are influenced by three plates very deficient in nebulae. If these plates were excluded, a normal distribution would represent the data reasonably well. The Shane and Wirtanen counts between latitudes $+40^\circ$ and $+50^\circ$ are greatly affected by the three large clouds in this region. But even if the areas of these clouds are omitted, the distribution has a strong skewness. The authors' counts between latitudes $+30^\circ$ and $+40^\circ$ are affected by local areas of galactic absorption and yield an excess of small values for $\log N$. When 1/30 of the largest and smallest counts were excluded, however, and the results were fitted to a partial normal curve in which the extremes were omitted, a good fit was obtained. The conclusion one may draw from this material is that, except where the counts are disturbed by unusual conditions, $\log N$ is represented very satisfactorily by a normal distribution function.

The values of σ_c/σ_r range from 2.2 to 2.4 except in regions strongly affected by large clouds of nebulae or by irregular galactic absorption. This large departure from unity strengthens the conclusion that nebulae tend to occur in clusters.

TABLE VII. COMPARISON OF OBSERVED AND RANDOM DISPERSIONS IN $\log N$

Authority	Lat.	No. of Areas	\bar{N}_c	$\overline{\log N}$	σ	σ_c	σ_r	$\frac{\sigma_c}{\sigma_r}$	P
Hubble*	45°	148	50.3	1.898	0.148	0.136	0.062	2.2	0.34
Mayall†	45	71	38.1	1.756	.230	.222	.074	3.0	<.01
S and W	>70	431	63.9	1.806	.154	.132	.054	2.4	.59
S and W	$60^\circ-70^\circ$	508	68.3	1.837	.148	.125	.053	2.4	.27
S and W	50-60	656	58.9	1.770	.156	.135	.057	2.4	.69
S and W	40-50	827	55.9	1.725	.208	.193	.060	3.2	<.01
S and W	30-40	671	32.1	1.484	.212	.197	.081	2.4	<.01
S and W	30-40**	649	32.1	1.490	0.197	0.182	0.081	2.3	0.54

* 1 hr. exposures with the 100-inch telescope.

† 1 hr. exposures with the 36-inch Crossley.

** The largest and smallest counts contributing 1/30 to the total were omitted.

XI. THE CLUSTER DENSITY FUNCTION

There appear to be two extreme structural types among the populous clusters, exemplified by the Virgo and the Coma clusters. The Virgo type is characterized by the absence of a strong central condensation and by lack of symmetry. Such clusters cannot readily be recognized at great distances where they become confused with the general background of nebulae, and therefore not many are known. They may be regarded as "open" clusters of nebulae. The Coma-type cluster is characterized by a strong central condensation and a tendency toward spherical symmetry. Such clusters can be recognized at great distances and are found in large numbers on the photographs. There may well be intermediate types, but at present our knowledge is too fragmentary to discuss their structure.

A considerable number of Coma-type clusters appear on the photographs of Area III. It is therefore worth while to investigate in a very preliminary fashion the manner in which the surface density in such clusters diminishes with distance from the center. Six of the clusters are suitable for such a study. All six are rather small or are somewhat disturbed by proximity to the edges of the plates, or to other clusters, and they therefore could not be investigated individually. The data were combined to form an average cluster whose density gradient could be determined.

The six clusters: For each cluster the center was located by inspection and the central count was recorded. The mean of the counts for the squares adjoining its four sides gave the value at $10'$ from the center. This process was continued outward by grouping conveniently increasing numbers of squares located within a sufficiently small range of distance until there was no longer an appreciable decrease in numbers of nebulae. Areas that were obviously disturbed by nearby clusters or groups of nebulae were avoided. A provisionally estimated value of the background was subtracted from the counts for each cluster, the resulting values were plotted against distance from the center, and a smooth curve was drawn to represent the points as well as possible. The curves for all six clusters were characterized by an initial rapid decrease in numbers of nebulae, followed by a very slow approach to zero. To reduce the observations to a common basis, abscissa and ordinate correction factors were derived for each cluster. The abscissa factor was determined by finding the abscissa at which the

TABLE VIII. SIX COMA-TYPE CLUSTERS

α 1950	δ 1950	Abscissa Factor	Ordinate Factor
12 ^h 16 ^m 3	+ 5° 35'	0.84	1.30
12 16.9	-13 05	1.06	1.37
12 39.0	- 4 35	0.90	1.40
14 24.5	+16 55	1.06	0.82
14 50.6	+16 55	1.06	0.64
14 52.6	+18 55	1.17	0.94

ordinate fell to one-third of its maximum value as read from the curves. The scale of abscissae was then multiplied by a number to make this "one-third point" the same for all clusters. A single ordinate factor was determined for each cluster to bring all six curves into the best agreement. When the individual observations corrected by these factors were plotted on a single chart, a large scatter was evident. The points were then grouped into eleven means or normal points on which the further discussion is based. The positions of the six clusters together with their coordinate factors are listed in Table VIII.

TABLE IX. CLUSTER DENSITY FUNCTION

Six Clusters				
r	n_r obs	O-C		
0.00	14.3*	+1.3*		
1.09	4.8	-0.2		
1.70	3.3	+0.1		
2.35	2.16	-0.08		
2.90	2.13	+0.40		
3.32	1.33	-0.16		
3.87	1.44	+0.22		
4.47	1.02	0.00		
5.28	0.83	+0.03		
6.52	0.61	+0.01		
7.97	0.41	-0.03		
Coma Cluster				
r	Plate 303		Plate 1613	
	n_r obs	O-C	n_r obs	O-C
0.0	30.0*	-23.0*	36.4*	-23.4*
1.0	20.2	+ 2.2	23.4	+ 2.3
1.4	11.5	- 0.9	15.9	+ 1.1
2.1	6.3	- 1.1	6.7	- 2.4
2.8	3.7	- 1.4	3.7	- 2.8
3.1	3.9	- 0.6	5.1	- 0.6
3.8	3.7	+ 0.4	4.5	+ 0.2
4.1	2.6	- 0.4	3.0	- 0.9
4.7	2.2	- 0.2	2.5	- 0.6
5.2	2.5	+ 0.5	3.4	+ 0.7
6.0	1.2	- 0.4	2.3	+ 0.1
6.3	2.7	+ 1.2	2.5	+ 0.5
7.6	1.3	+ 0.2	1.4	- 0.1
7.8	1.3	+ 0.3	1.9	+ 0.5
8.8	0.8	0.0	1.3	+ 0.1
9.7	0.8	+ 0.1	0.9	- 0.1
9.9	0.6	- 0.1	1.0	+ 0.1
10.8	0.6	0.0	0.6	- 0.3
12.3	0.4	0.0	0.9	+ 0.3
12.9	0.4	0.0	0.8	+ 0.2

* For $r = 0$ the observed values are the numbers of nebulae in a $10'$ square corrected for background. The computed values are the numbers within a circle of 100 square minutes area.

The average number of background nebulae subtracted from the counts was 1.5 nebulae per $10'$ square. This value is certainly too large since it is based on the distance at which the counts were terminated. With the evident slow decrease in numbers of nebular outward from the center a greater distance should be used to establish the true background density. For each cluster several areas, two or more degrees from the center, were located in which there seemed to be little or no effect of nebular aggregations. The background densities derived from these areas gave a mean value of 1.1 nebulae per $10'$ square. Each of the eleven normal points was accordingly increased by 0.4. The first and second columns of Table IX give, respectively, distances, r , in units of $10'$ from the center of the average cluster, and the corresponding corrected surface densities.

Two plates of the Coma cluster (α 1950 = $12^{\text{h}} 57^{\text{m}} 5$; δ 1950 = $+28^{\circ} 20'$), which lies just off the northern edge of Area III, were investigated separately.

The Coma Cluster, Plate 303. This plate, a two-hour exposure centered on the cluster, was taken without the grating. Figure 10 represents the nebular density distribution by contours whose interval is four nebulae per ten minute square. The contour for two nebulae per ten minute square is shown by the broken line. In drawing the contours the counts were averaged by fours in the usual manner. However, the numbers on the chart give the actual counts. It

is apparent that there is a subsidiary concentration of nebulae southwest of the cluster center. This grouping may be a secondary feature of the cluster or it may represent an independent aggregation. The area included in the rectangle outlined by the broken lines was therefore not used in discussing the density function. With this omission the cluster approximates circular symmetry.

The position of the largest count, 31, was adopted as the center of the cluster. The true center probably lies somewhere between counts 31 and 22, but this centering error should appreciably effect only the central count. At $130'$ from the center the average number of nebulae per ten minute square reached 1.4 and was no longer decreasing noticeably. This distance seemed to correspond to the average distances at which the counts on the six clusters were terminated. Consequently, as with the 6 clusters, the terminal value was decreased by 0.4 to give a background count of 1.0. The surface density corrected for this background is given in the second column of the lower part of Table IX.

The Coma Cluster, Plate 1613. This plate was taken on the regular program and includes the cluster centered $105'$ south and $35'$ west of the plate center. Figure 11, the contour representation for this plate, indicates a close similarity to the chart for Plate 303 but with a fainter limiting magnitude. If a Number 6 contour were drawn on Plate 303, it would correspond rather closely to the Number 8 contour on Plate 1613. The

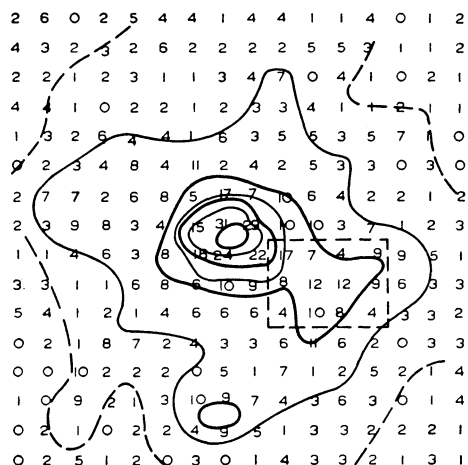


Fig. 10. Plate 303

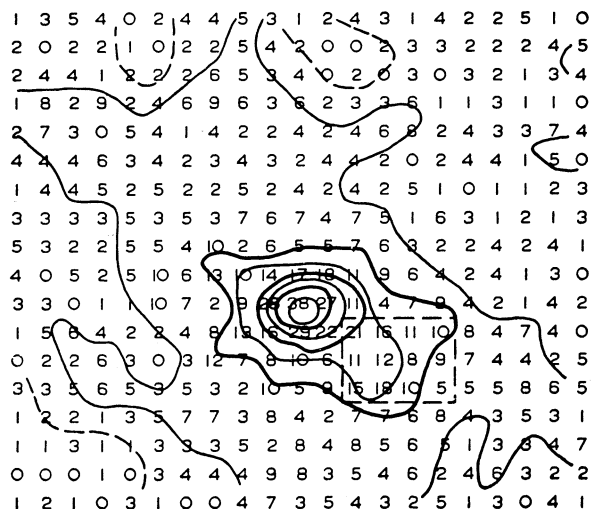


Fig. 11. Plate 1613

Figures 10 and 11. Contour maps of the Coma cluster of nebulae, based on smoothed counts by $10'$ squares.

latter plate has a uniformly higher density of nebulae, with 2.2 or 2.3 nebulae per ten minute square at 130' from the cluster center. Since the cluster was considerably south and west of the plate center, it was possible to find relatively undisturbed areas of background near the north edge of the plate. The average count in these areas was 1.6 nebulae per square degree. Correction for this background density was applied to the counts with the results tabulated in the fourth column of the lower part of Table IX.

Empirical formula of de Vaucouleurs. It has been shown by G. de Vaucouleurs that a formula equivalent to $\log n_r = a(r^k + b)$ represents with remarkable fidelity the observed distribution of brightness in elliptical nebulae.¹¹ His value $b = -1$ corresponds to the adoption of a special unit of brightness in his applications. De Vaucouleurs¹² also applied the formula to nebular counts by Zwicky¹³ in three clusters of nebulae and obtained an excellent representation. The formula was applied to our observations with the results represented by the O-C columns of Table IX and the constants in Table X. The

TABLE X. CONSTANTS FOR DE VAUCOULEURS' FORMULA

	a	b	r_0	Neb. inside r_0
Six Clusters	-1.595 (-1.738)	-1.458 (-1.426)	19.01 (13.48)	405 (290)
Coma Cl., Plate 303	-1.855 (-1.938)	-1.677 (-1.652)	10.38 (8.71)	738 (642)
Coma Cl., Plate 1613	-1.745 (-1.807)	-1.759 (-1.738)	13.25 (11.54)	1153 (972)

quantities in Table X not enclosed in parentheses are based on the observational data in Table IX; those in parentheses are derived from n_r diminished throughout by 0.1. This change corresponds to raising the assumed background by 3.6 nebulae per square degree, an amount within the uncertainties of its determination. The column headed r_0 gives the distance from the center of each cluster within which half the total number of nebulae should lie, according to the formula. The number within the distance r_0 is given in the last column of the table. The total number of nebulae to $r = \infty$ is twice this value for each cluster. The constants in Table X were determined without using the observational data for $r = 0$. Clearly, the equation does not fit at the immediate center of the Coma cluster, but elsewhere the agreement is good.

The important point to be noted is that the density of nebulae in a Coma-type cluster, and

the brightness of an elliptical nebula, decrease outward in much the same manner.

XII. CLOUDS OR MULTIPLE CLUSTERS

In the list of twenty-five clusters of nebulae published by Shapley,¹⁴ he noted the occurrence of two double groups and one triple group. He suggested that these multiple groups were physically connected because of the proximity of the members both in direction and in distance as indicated by their distribution in apparent magnitude.

In Area III there occur three large multiple clusters or clouds of nebulae and several smaller ones. Contour maps of six of these clouds are illustrated in more detail in Figures 12 to 16 than in the main chart, Figure 2. The corrected counts by quarter instead of whole square degrees were smoothed by fours and then contours were drawn through the smoothed points. The contour interval is ten nebulae per square degree. It is apparent that each cloud consists of two or more comparable clusters with subsidiary condensations, except for the cloud at $\alpha = 14^h 25^m$, $\delta = +16^\circ 7'$. An examination of the unsmoothed counts for this cloud shows that the ridge extending to the northwest is produced by two secondary aggregations of nebulae whose identities were lost through the smoothing process.

Data for the six clouds are given below. All positions are for 1950. Distances are given on the scale proposed by Baade at the Rome I.A.U. meeting in September 1952.

1. Figure 12: $\alpha = 12^h 16^m$, $\delta = +4^\circ 8'$. In 14.8 square degrees 505 nebulae above a background of 80 nebulae per square degree. Two main centers of condensation at $\alpha = 12^h 15^m$, $\delta = +4^\circ 0'$; $\alpha = 12^h 16^m$, $\delta = +5^\circ 5'$.

2. Figure 13: $\alpha = 12^h 54^m$, $\delta = -15^\circ 2'$. In an area of 25 square degrees 1388 nebulae above a background of 80. Distance of the southernmost condensation based on magnitude distribution according to Shapley,¹⁴ 58×10^6 parsecs. Three major condensations at $\alpha = 12^h 51^m$, $\delta = -15^\circ 2'$; $\alpha = 12^h 55^m$, $\delta = -17^\circ 2'$; $\alpha = 12^h 55^m$, $\delta = -13^\circ 2'$. Also two minor condensations.

3. Figure 14: $\alpha = 14^h 25^m$, $\delta = +16^\circ 7'$. In 6.5 square degrees 214 nebulae above a background of 88. One major condensation at $\alpha = 14^h 25^m$, $\delta = +16^\circ 7'$. Two minor condensations at $\alpha = 14^h 20^m$, $\delta = +17^\circ 8'$; $\alpha = 14^h 16^m$, $\delta = +18^\circ 8'$.

4. Figure 14: $\alpha = 14^h 52^m$, $\delta = +17^\circ 9'$. In 8.2 square degrees 359 nebulae above a background

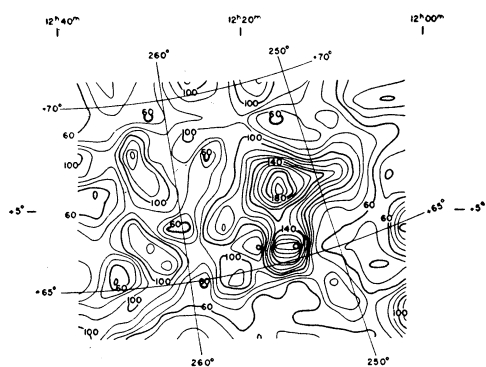


Fig. 12

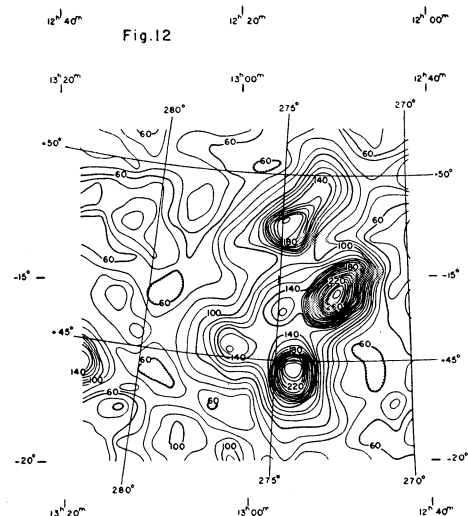


Fig. 13

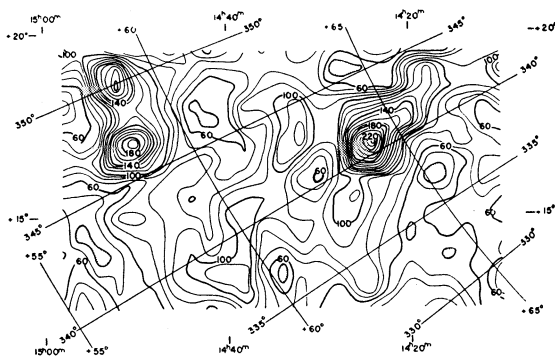


Fig. 14

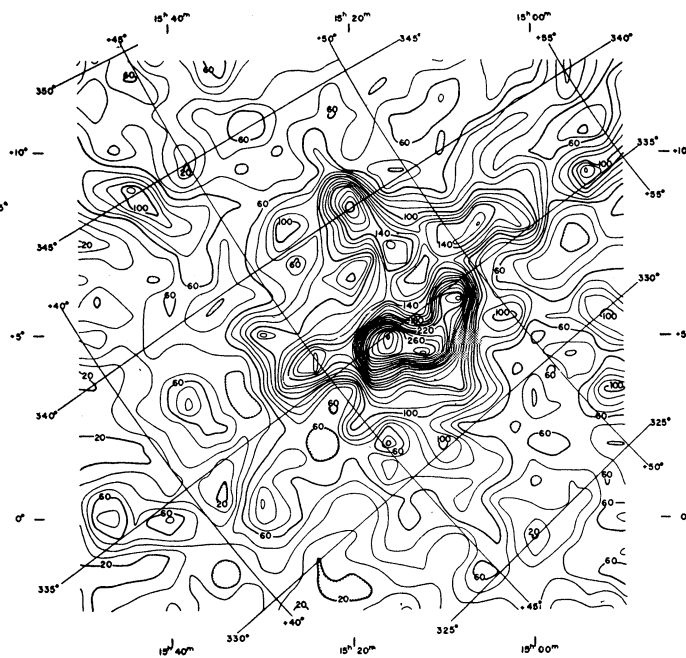


Fig. 15

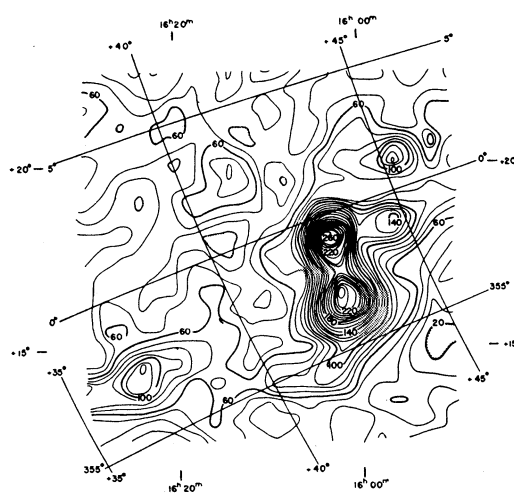


Fig. 16

Figures 12–16. Contour maps of clouds of nebulae, based on smoothed counts by 0.5° squares.

of 88. Two main condensations at $\alpha = 14^h 51^m$, $\delta = +17^\circ 0'$; $\alpha = 14^h 53^m$, $\delta = +18^\circ 8'$.

5. Figure 15: $\alpha = 15^h 12^m$, $\delta = +5^\circ 2'$. In 52 square degrees 2810 nebulae above a background of 68. Three major condensations at $\alpha = 15^h 09^m$, $\delta = +6^\circ 0'$; $\alpha = 15^h 11^m$, $\delta = +4^\circ 8'$; $\alpha = 15^h 17^m$, $\delta = +4^\circ 5'$. Three to five minor centers of con-

densation. Spectrograms of two nebulae at $\alpha = 15^h 20^m 4$, $\delta = +8^\circ 47'$ in a minor condensation, kindly obtained by Dr. Mayall to estimate the distance of the cloud, give red shifts $+10,500$ and $+10,400$ km/sec; with the corresponding distance 39×10^6 parsecs.

6. Figure 16: $\alpha = 16^h 02^m$, $\delta = +17^\circ 0'$. In 20.2